



CTU

**CZECH TECHNICAL
UNIVERSITY
IN PRAGUE**



Groundwater hydraulics

2

Definition of properties

Continuous (macroscopic) approach

Observation of water fluxes in porous medium is possible at focus on level

Molecular

Microscopic

Macroscopic

Molecular scale: movement of water and solute molecules

Microscopic – at pore scale

real phases (water, air, solids) is replaced by microcontinuum which fills partial spaces,

There is one microcontinuum at one time and space only

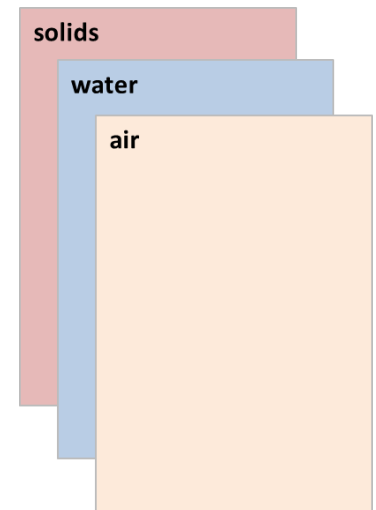
Macroscopic scale

all phases are mutually overlapped

in fictitious macrocontinua

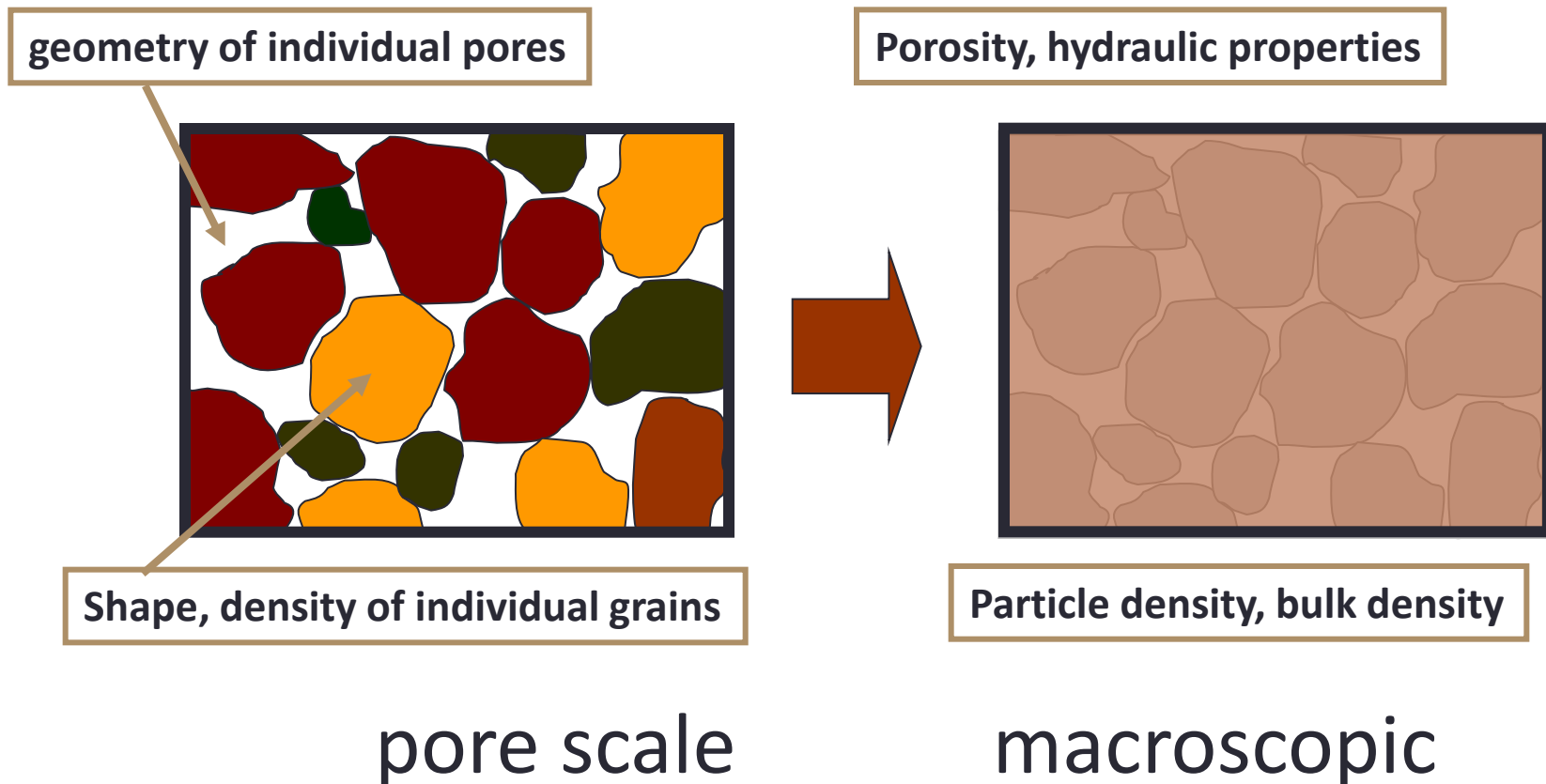
filling the flow zone entirely

at one space, there is unlimited number of macrocontinua

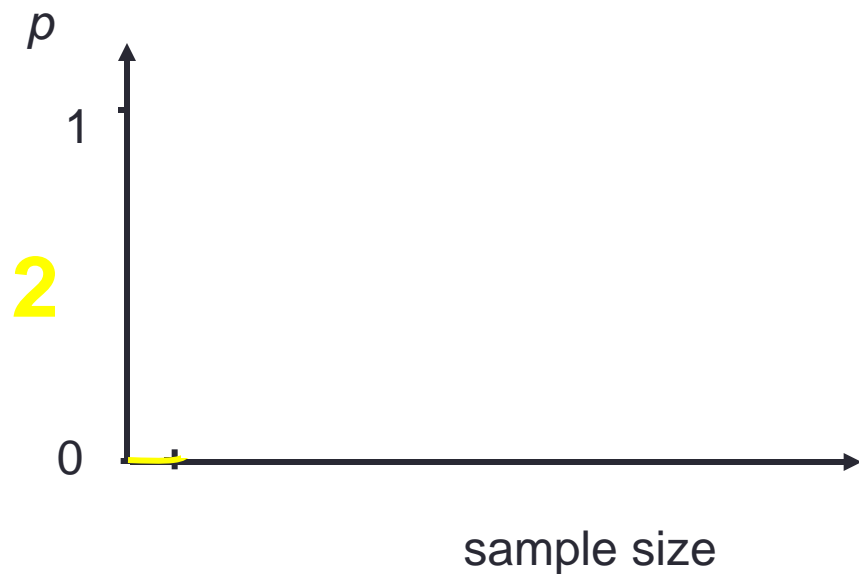
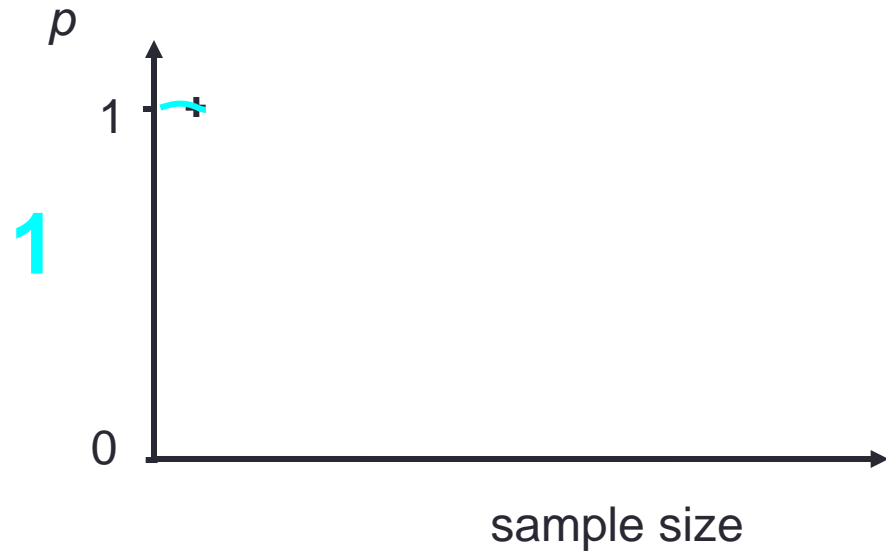
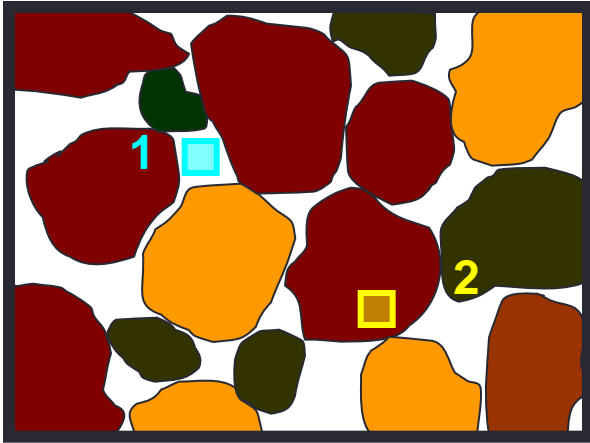


From microscopic to macroscopic approach

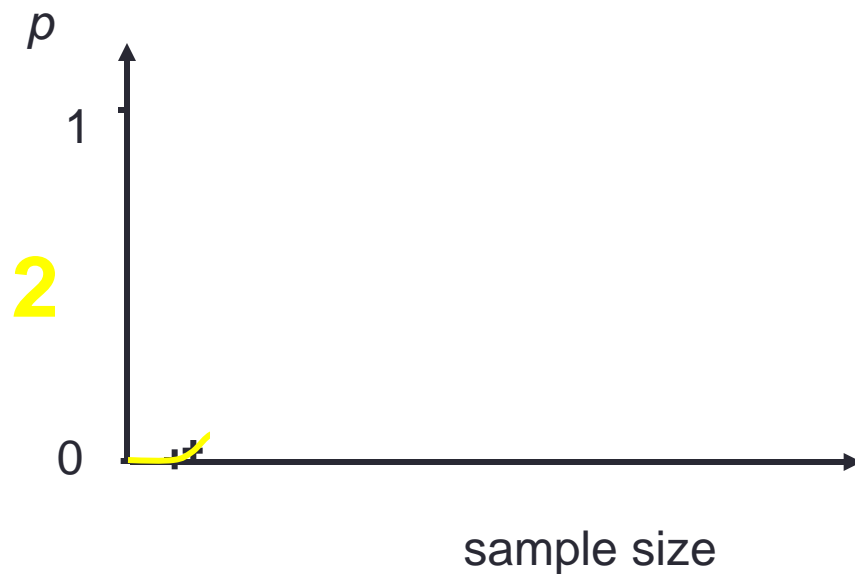
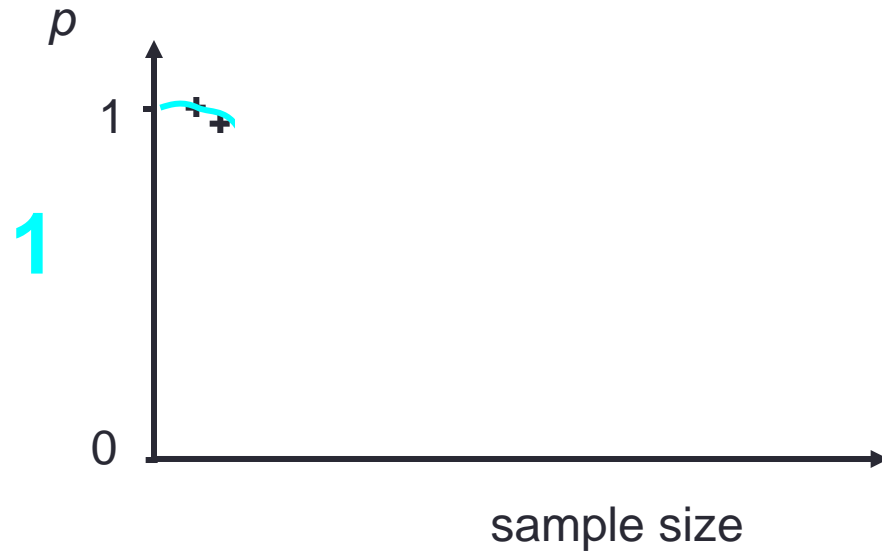
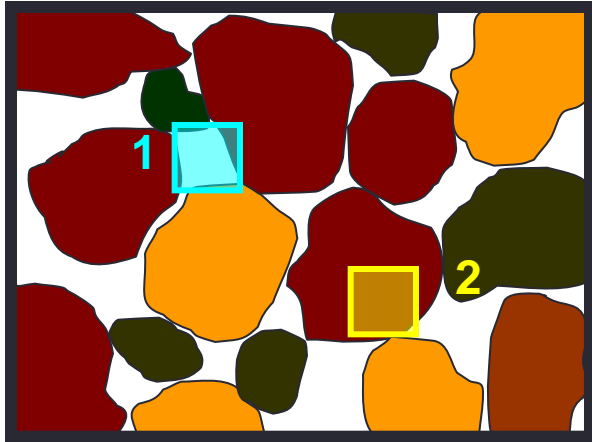
Description of the water flow and solute transport in soil (porous media) is (so far) not possible at the pore scale level. Therefore the **macroscopic approach** is used.



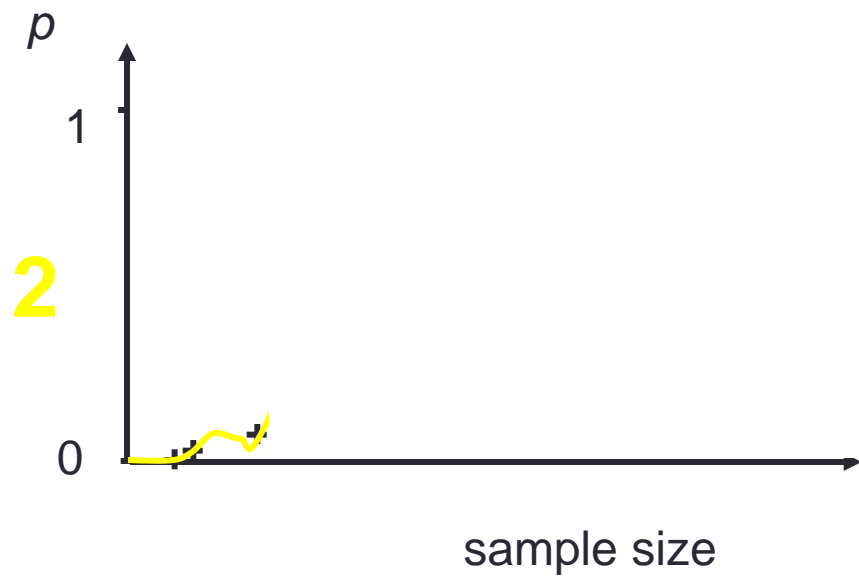
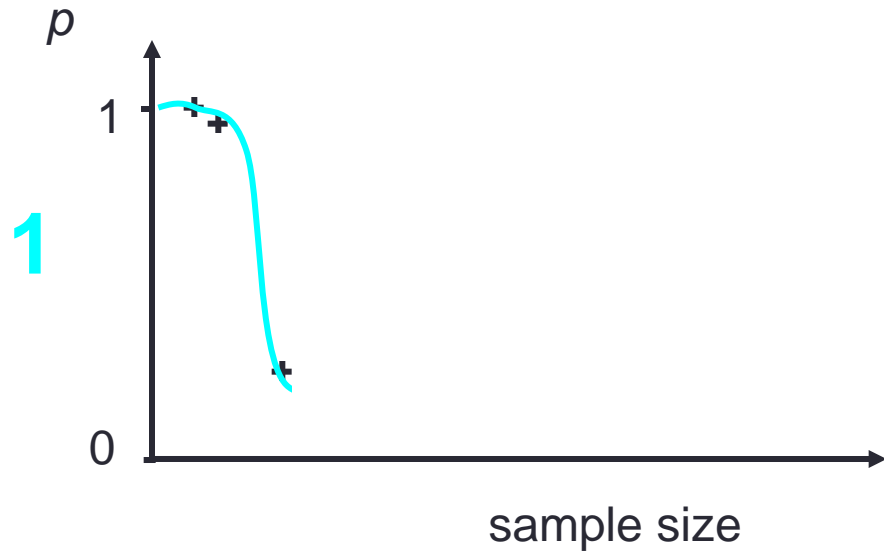
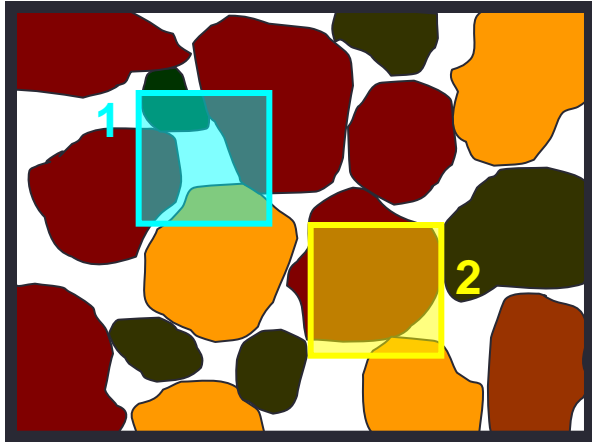
Representative elementary volume (REV)



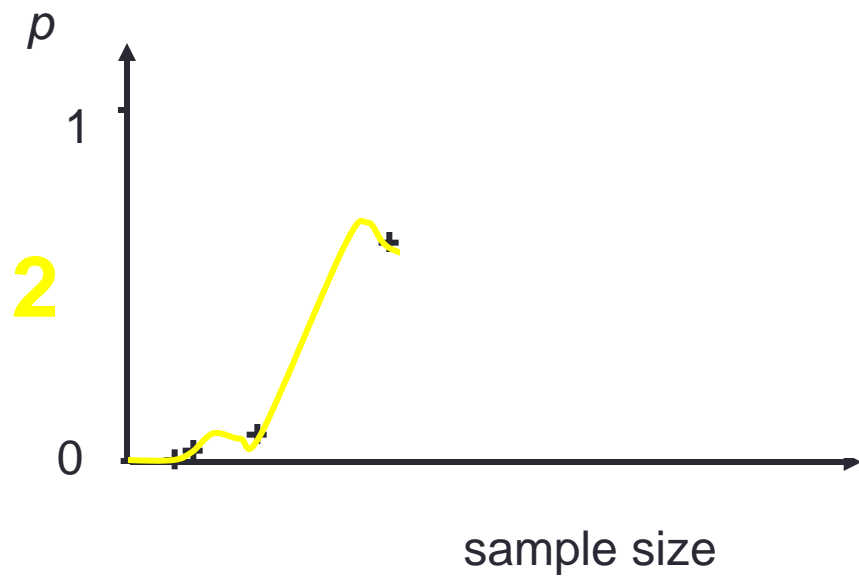
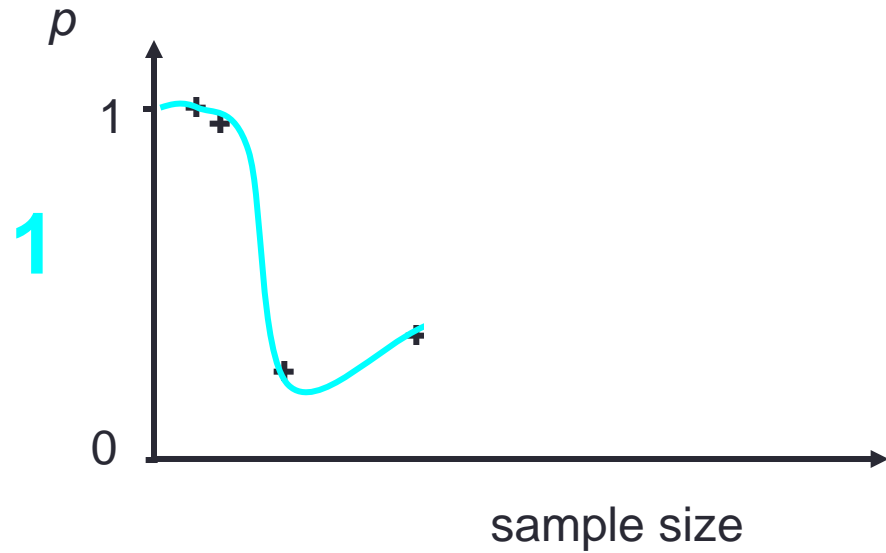
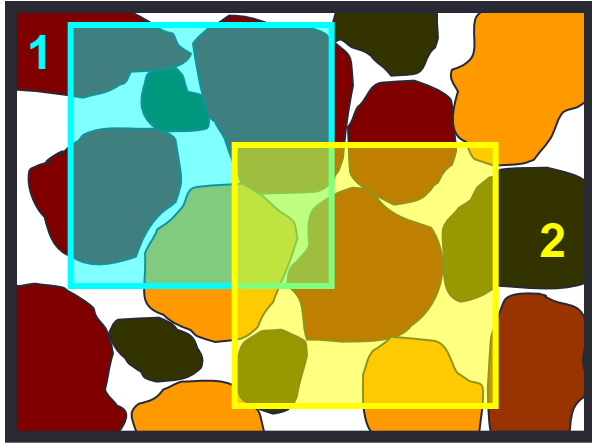
Representative elementary volume (REV)



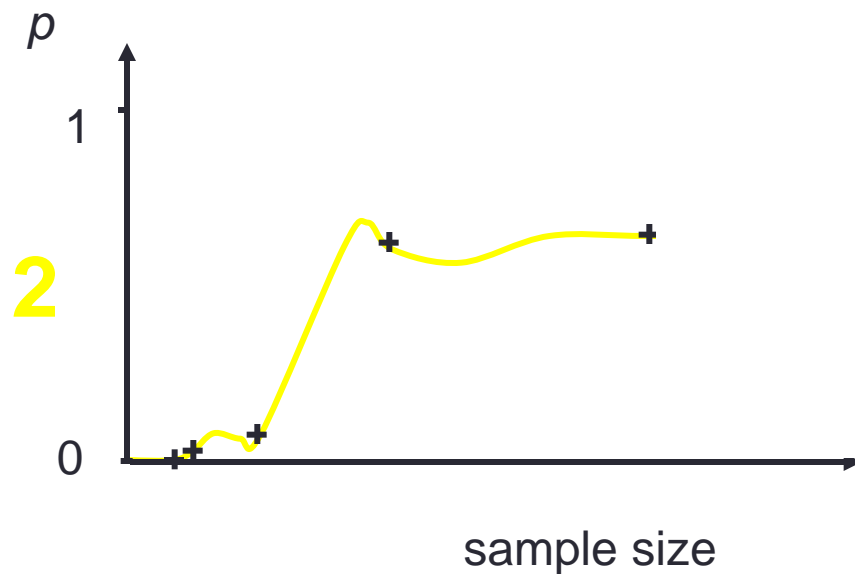
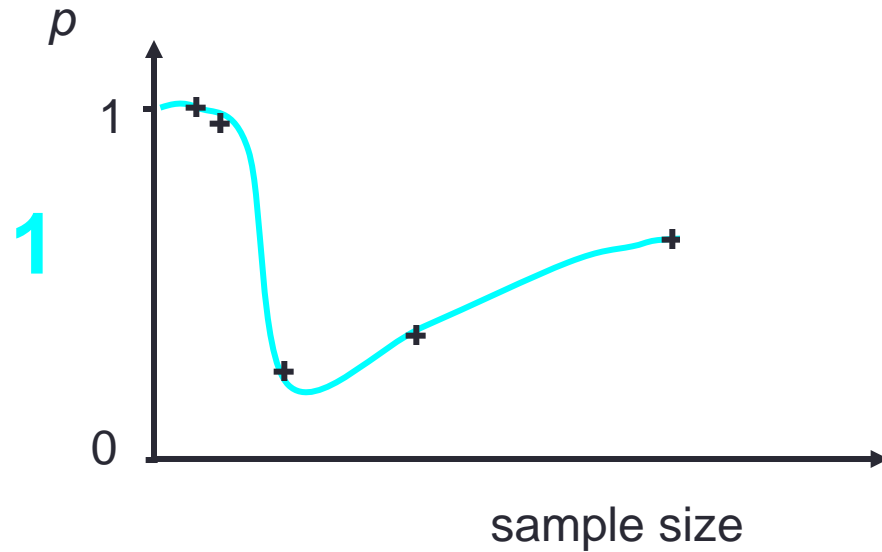
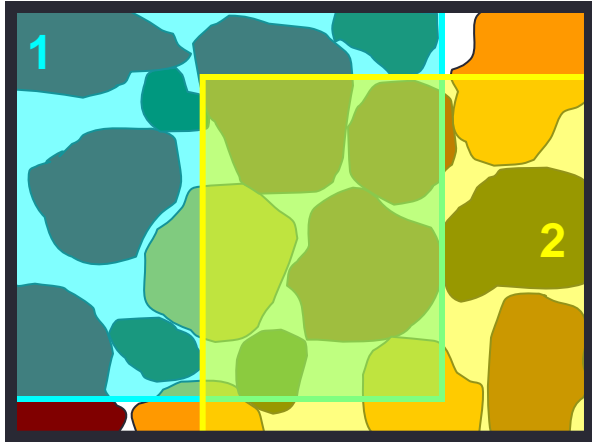
Representative elementary volume (REV)



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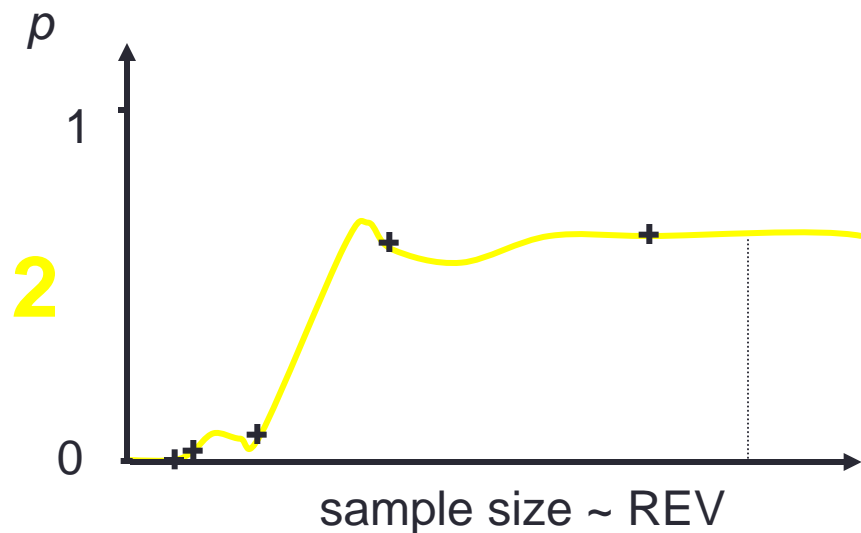
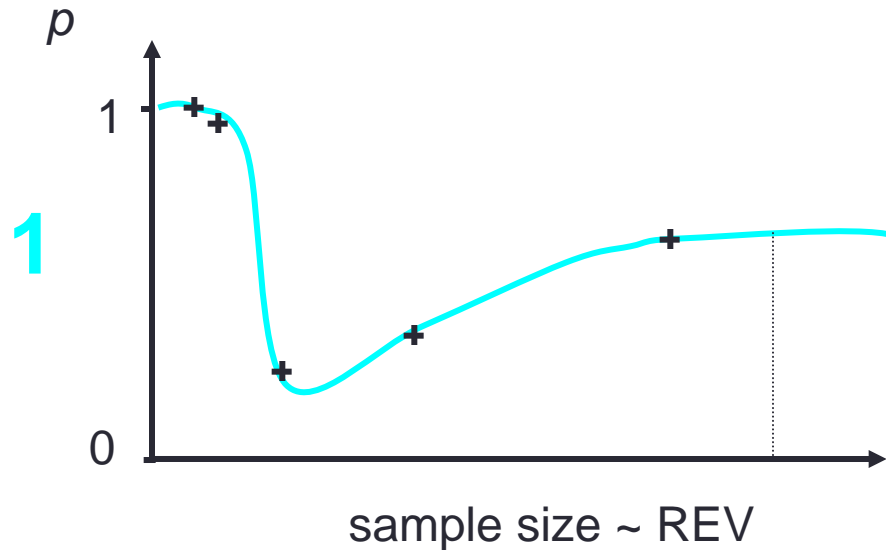
Representative elementary volume (REV)



Representative elementary volume (REV)

REV (Representative Elementary Volume) is the smallest volume over which a measurement can be made that will yield a value representative of the whole

REV depends on soil heterogeneity. REV of soils is mostly in range of $10^2 - 10^3 \text{ cm}^3$.



From microscopic to macroscopic

By averaging through representative elementary (REV) volume where microscopic P^{mic} are transformed to macroscopic P^{mac} (P is any of the properties of the phase (density, porosity...))

REV – is a volume in orders of magnitude higher than characteristic pore size and orders of magnitude smaller than area of interest

Averaging at entire REV:

$$\bar{P}_\alpha^{mac} = \frac{1}{V} \int_V P_\alpha^{mic} dV$$

Averaging at part of the volume with phase α :

$$P_\alpha^{mac} = \frac{1}{V_\alpha} \int_{V_\alpha} P_\alpha^{mic} dV$$

Relation of those above



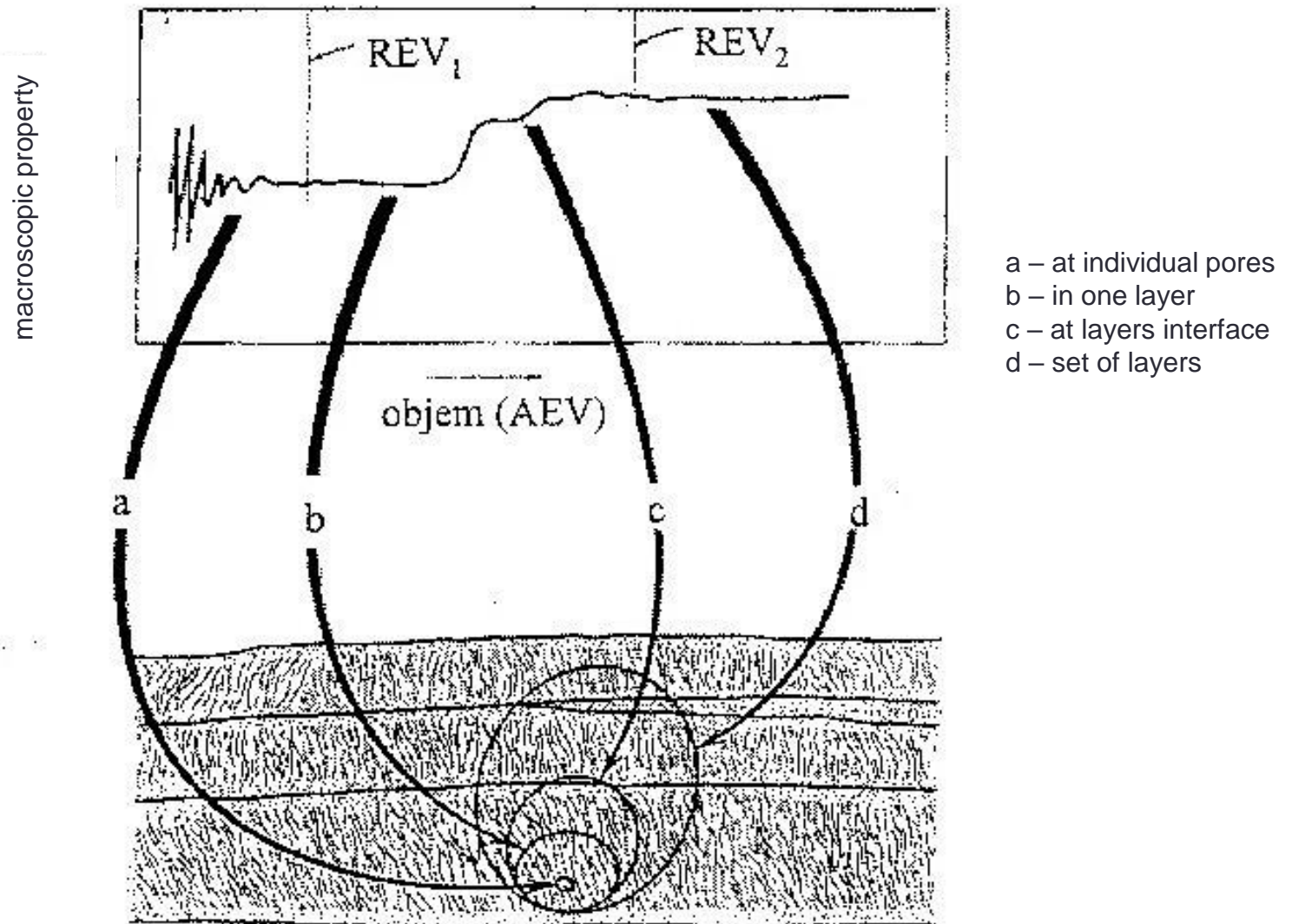
where

$$\varepsilon_\alpha = \frac{V_\alpha}{V}$$

Is volumetric ratio of phase α

Value of macroscopic property is assigned at center of REV. Running REV through the area of interest, continuous field of P values is obtained

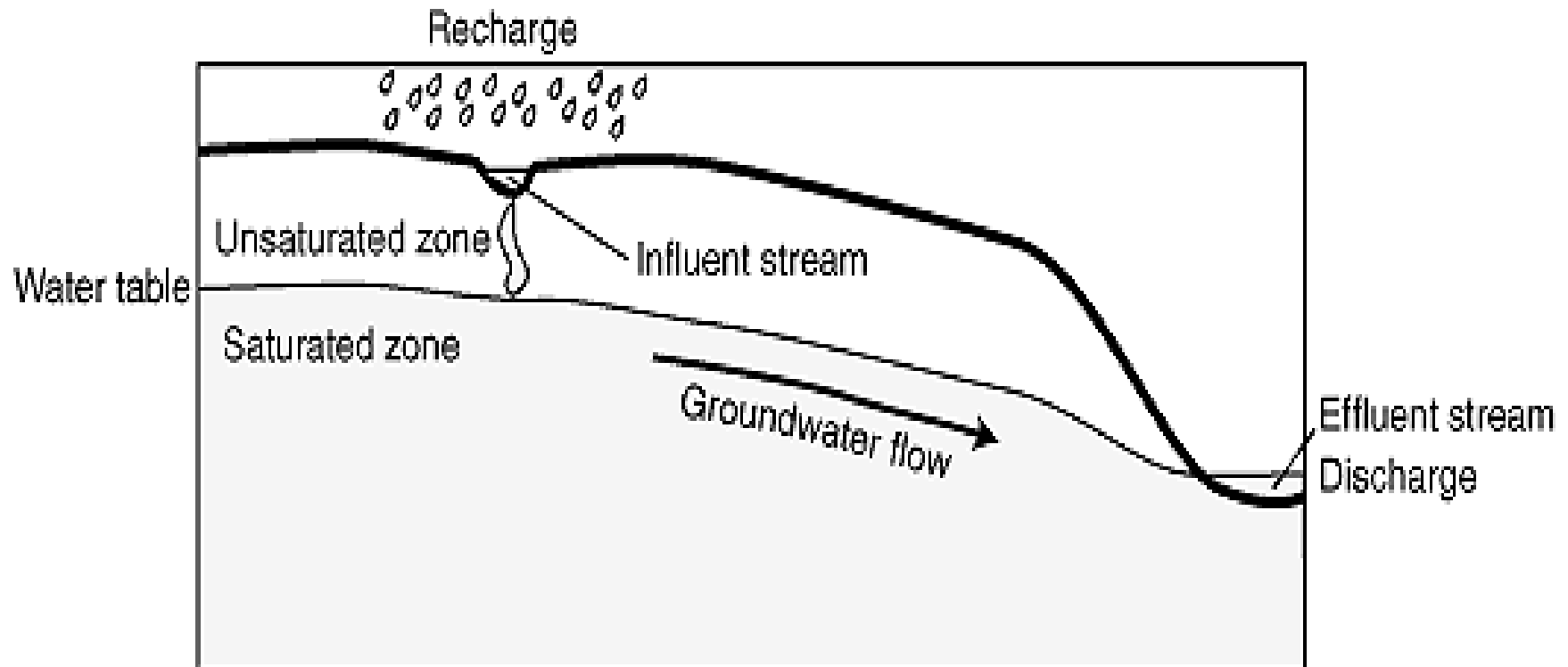
Macroscopically heterogeneous environment



Fundamentals for groundwater movement

Groundwater movement as part of the hydrological cycle occurs from areas of natural or artificial infiltration (recharge) of water to areas of natural or artificial discharge (stream or pumping well). While moving, groundwater overcomes resistance of the environment – inner friction of water and friction of water on grains, resulting in loss of mechanical energy of flowing water. **Ability of water to move in porous medium is determined by its mechanical energy.**

Potential of the liquid is a measure of this ability



Fundamentals for groundwater movement

Flow potential = mechanical energy of water weight unit
in saturated flow in porous media consist of two parts
gravity and pressure potential

Gravity potential is defined as energy necessary to move
the weight unit of water from the zero level to level z

$$\psi_1 = g z$$

Pressure potential is defined ad energy necessary to increase pressure
From p_0 na p :

$$\psi_2 = \int_{p_0}^p \frac{dp}{\rho}$$

Gravity and pressure
potential combined

$$\Phi = g z + \int_{p_0}^p \frac{dp}{\rho}$$

Fundamentals for groundwater movement

Flow potential for incompressible fluid ($\rho = \text{const.}$):

$$\Phi = g z + \frac{p - p_0}{\rho}$$

Water pressure is typically assigned at zero level equal to atmospheric pressure p_0 , then

flow potential is defined as

$$\Phi = g z + \frac{p}{\rho}$$

Water flow in between two points in porous space occurs in case of different potentials of water and simultaneously, there is continuous passage permeable for water. Water moves from level of higher to lower potential.

Groundwater hydraulics typically describes potential as hydraulic head H

$$H = \frac{\Phi}{g} \qquad H = z + \frac{p}{\rho g}$$

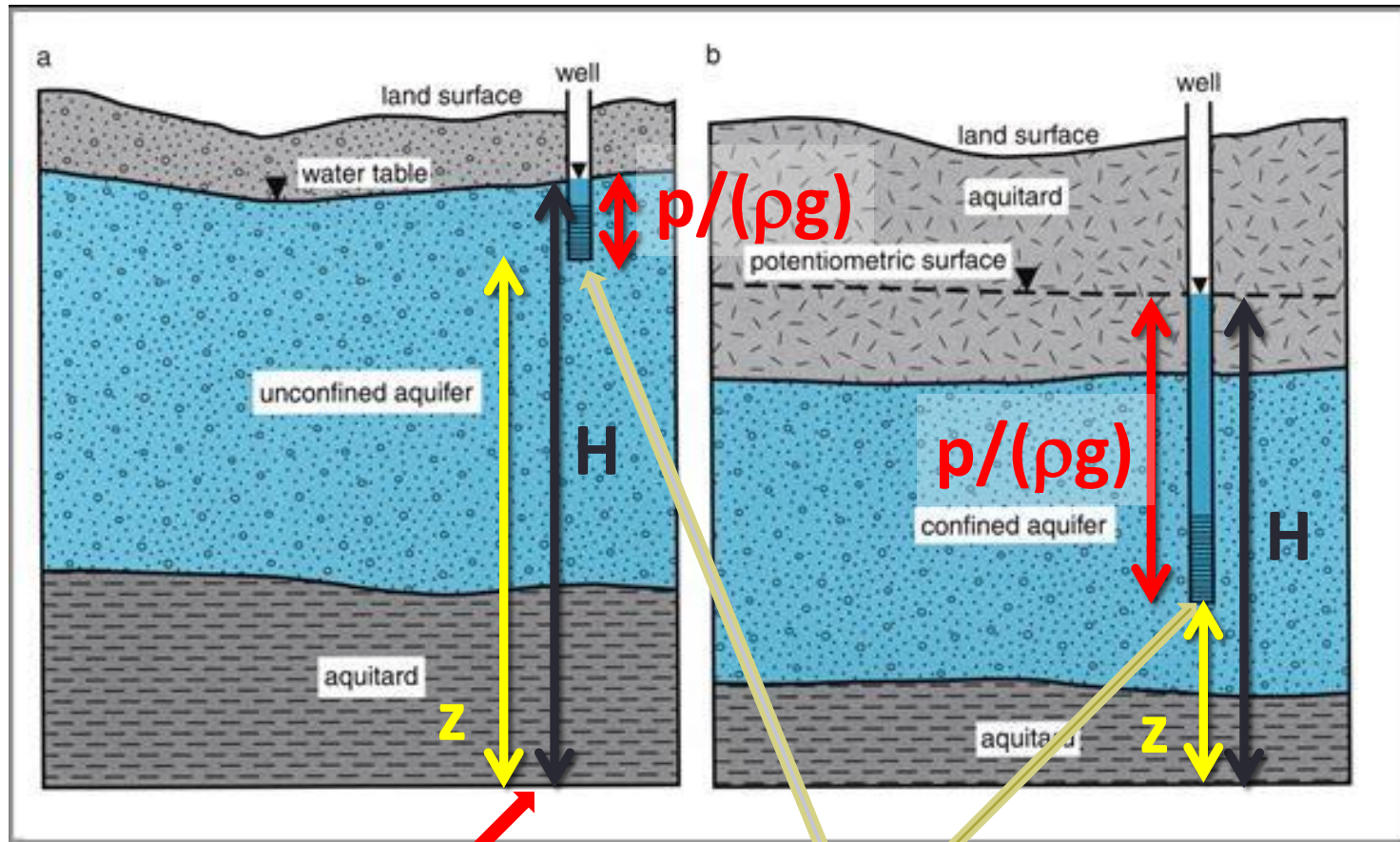
$$p = h_p \rho g ,$$

Hydraulic head is summation of geodetic and pressure head

Measurement of hydraulic head – piezometer

free head

pressurized head



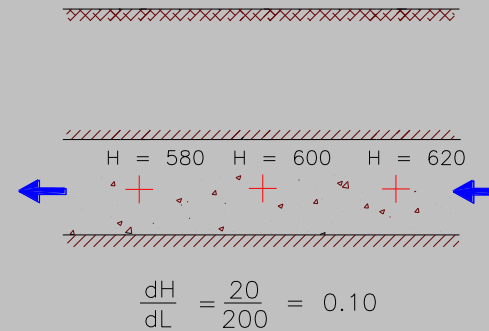
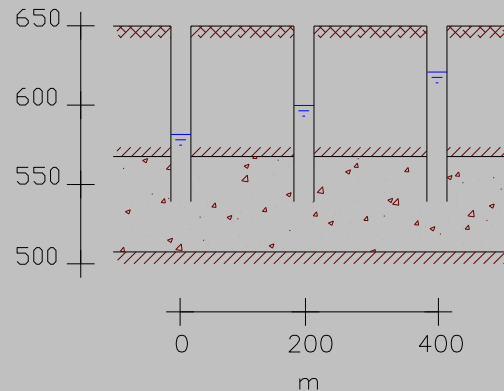
datum $z=0$

measured point

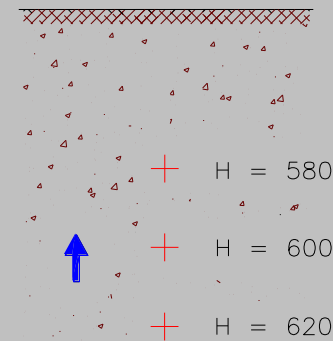
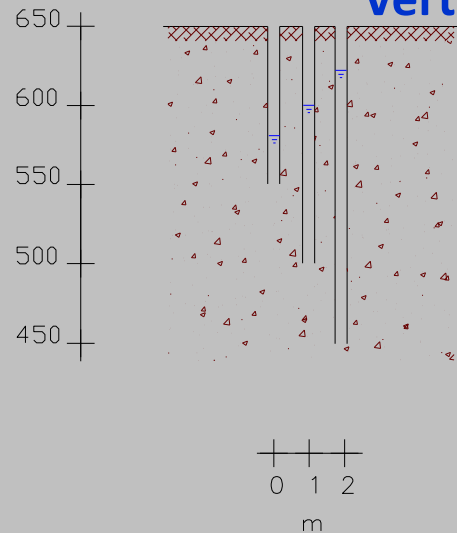
$$H = \frac{\Phi}{g} \quad H = z + \frac{p}{\rho g}$$

Determination of groundwater flow direction based on group of piezometers

Horizontal direction of flow



Vertical flow direction



$$\frac{dH}{dL} = \frac{20}{50} = 0.40$$

Groundwater levels and water flow description

Free (phreatic) groundwater surface map of hydroisohypse

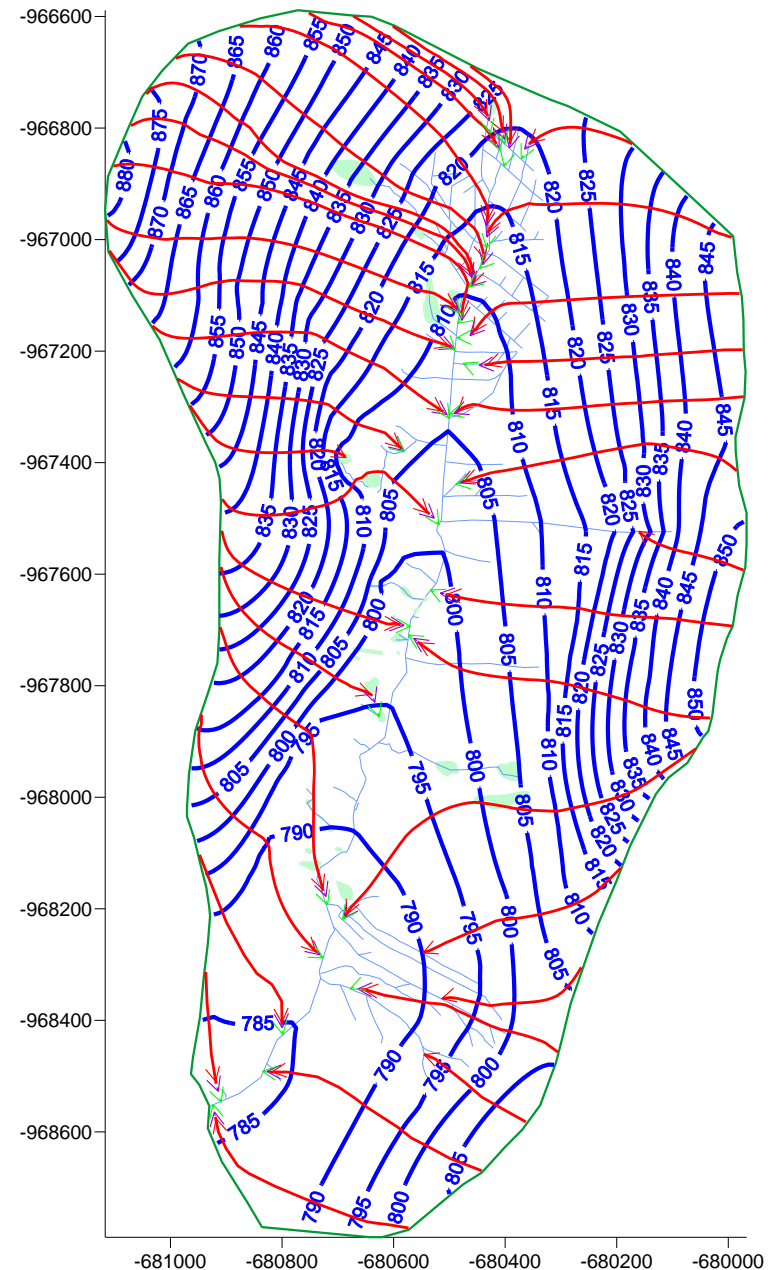
HYDROIZOHYPSE = connects points of the same level of free groundwater at the same time

Pressurized (confined) aquifer - map of piezometric heads

Piezometric surface connects points of the same level of piezometric level of groundwater at the same time

Trajectory - map of travel directions of groundwater considering flow time history

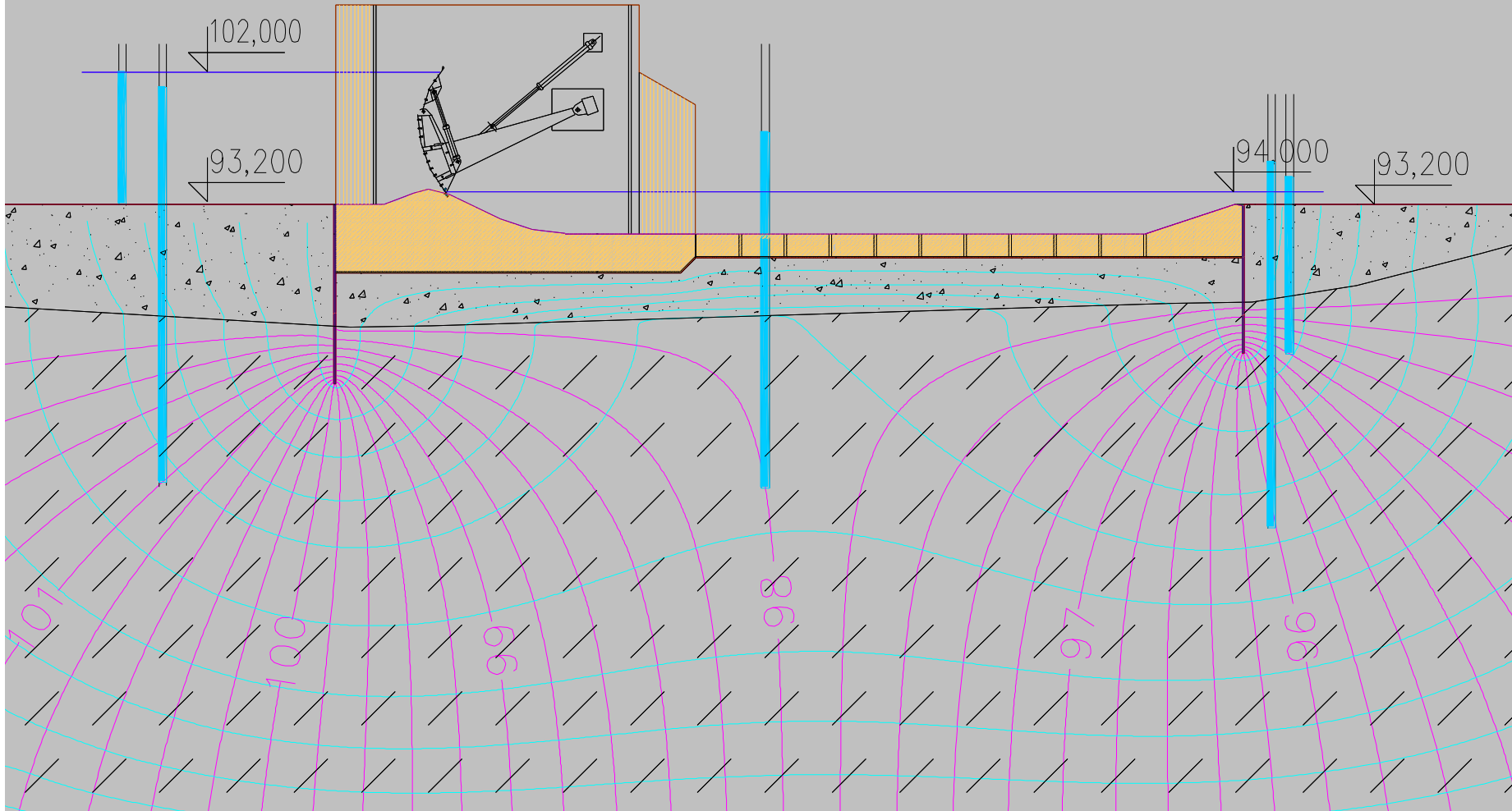
(for assumption of steady state flow perpendicular to piezometric heads)



Groundwater under river construction (segment weir)

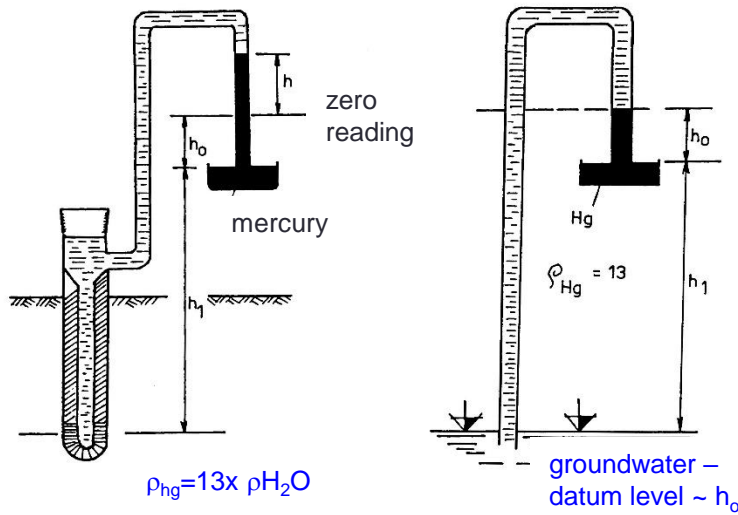
piezometric heads (equipotentials)

flowlines

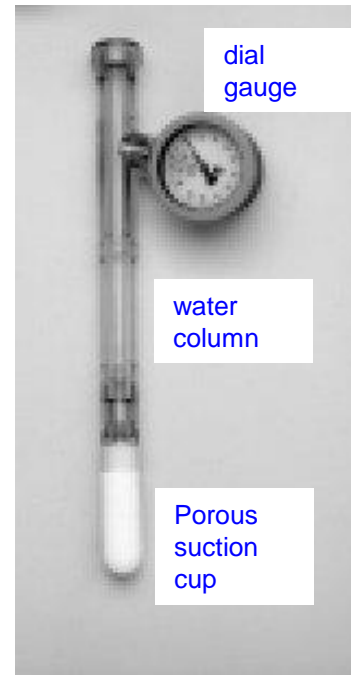


Capillary potential – pressure in vadose zone

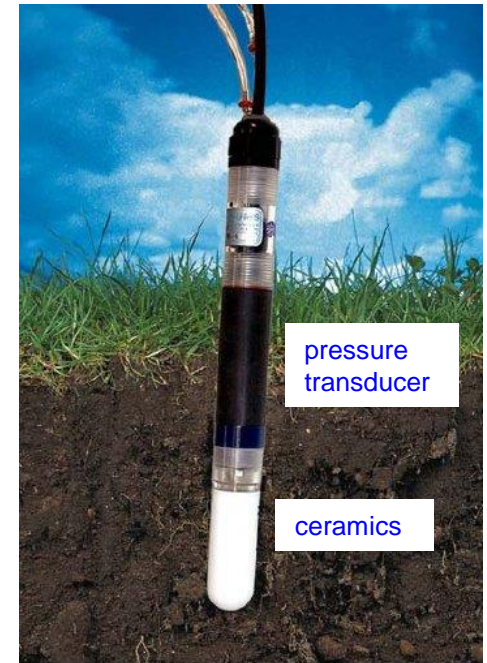
Thin tube inserted in the soil. Capillary potential sampled in the porous suction cup, but measured at the gauge above it with linear increase of suction
Pressure head can be referenced at the surface. Generally total potential (in pressure head) equals to $H = p/(\rho g) - z$. ($h = p/(\rho g)$: capillary, z : vertical distance)



tensiometer with mercury manometers



dial gauge



transducer

For details see Soil physics and soil science course

Groundwater vocabulary

Hydrogeological structure

Structurally and geologically defined environment, where infiltration, accumulation and drainage of groundwater occurs

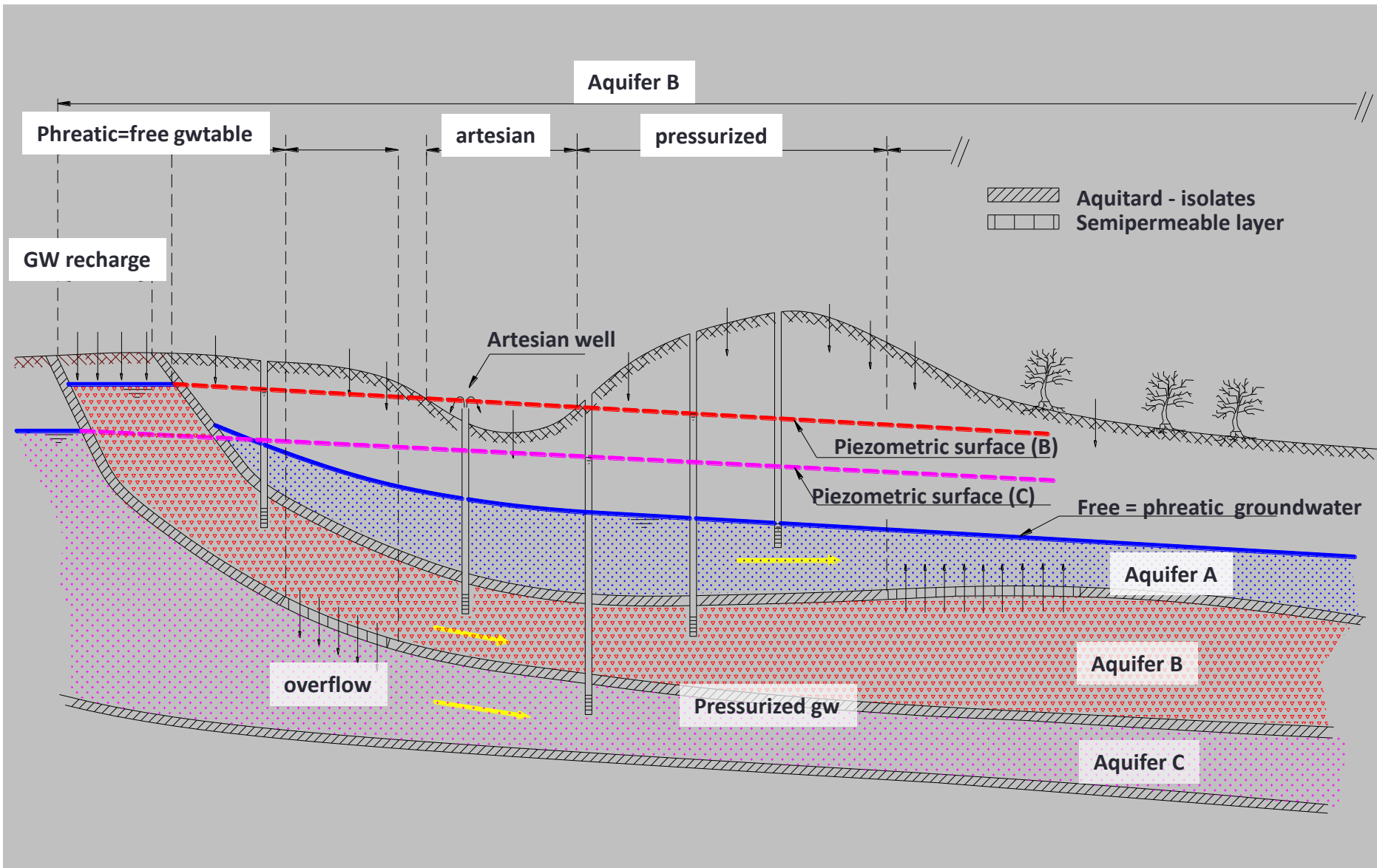
Aquifer

Geological body, with permeability for water significantly higher than surrounding environment, enabling gravity water to move much more freely under same hydraulic (pressure) conditions

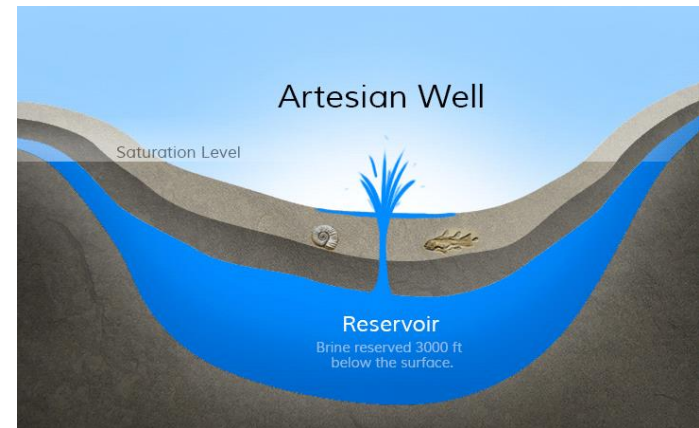
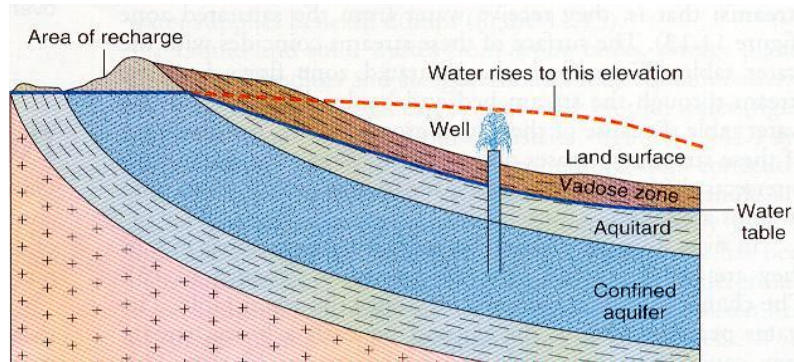
Aquitard

Geological body, with permeability for water significantly lower than surrounding environment, non-enabling gravity water to move, or enabling to move much worse under same hydraulic (pressure) conditions

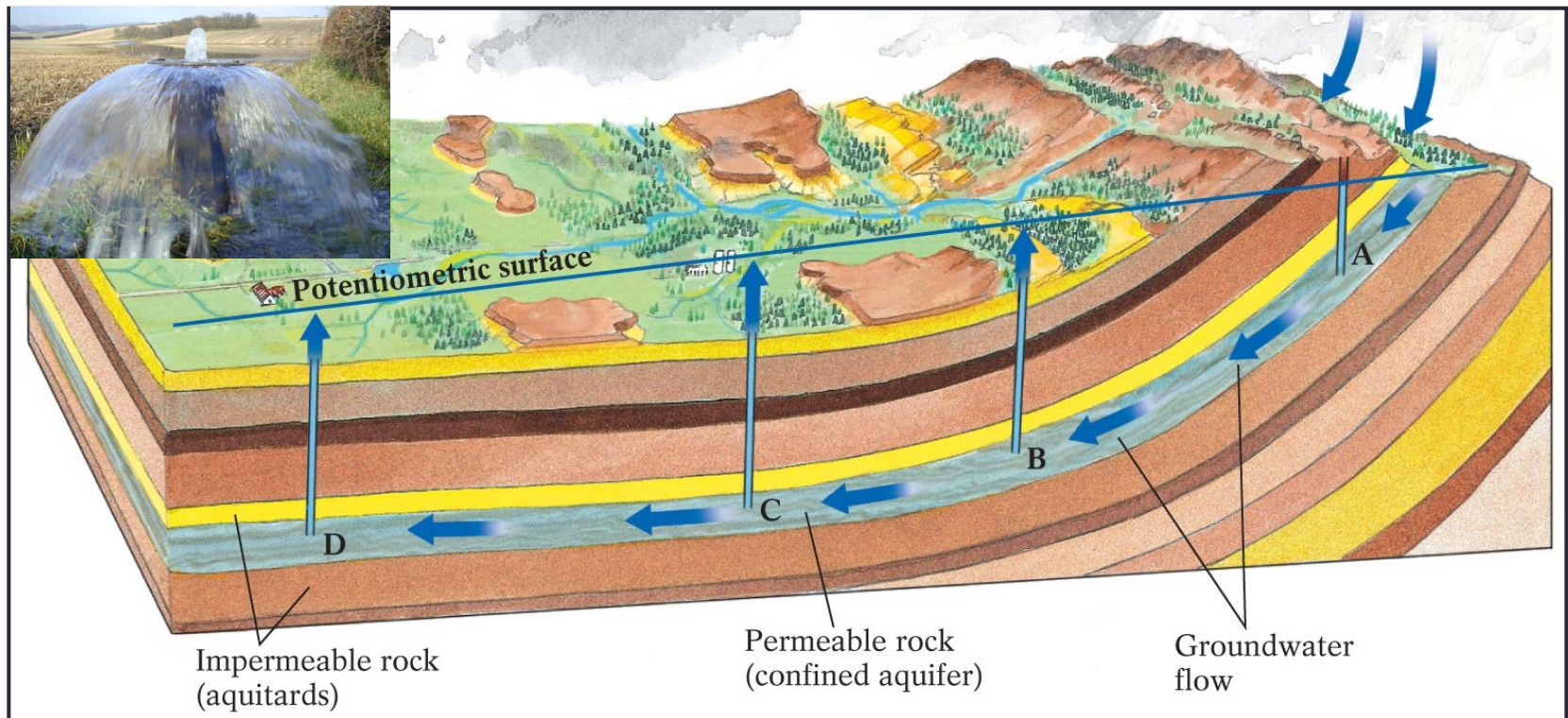
Types of aquifers



Artesian aquifer



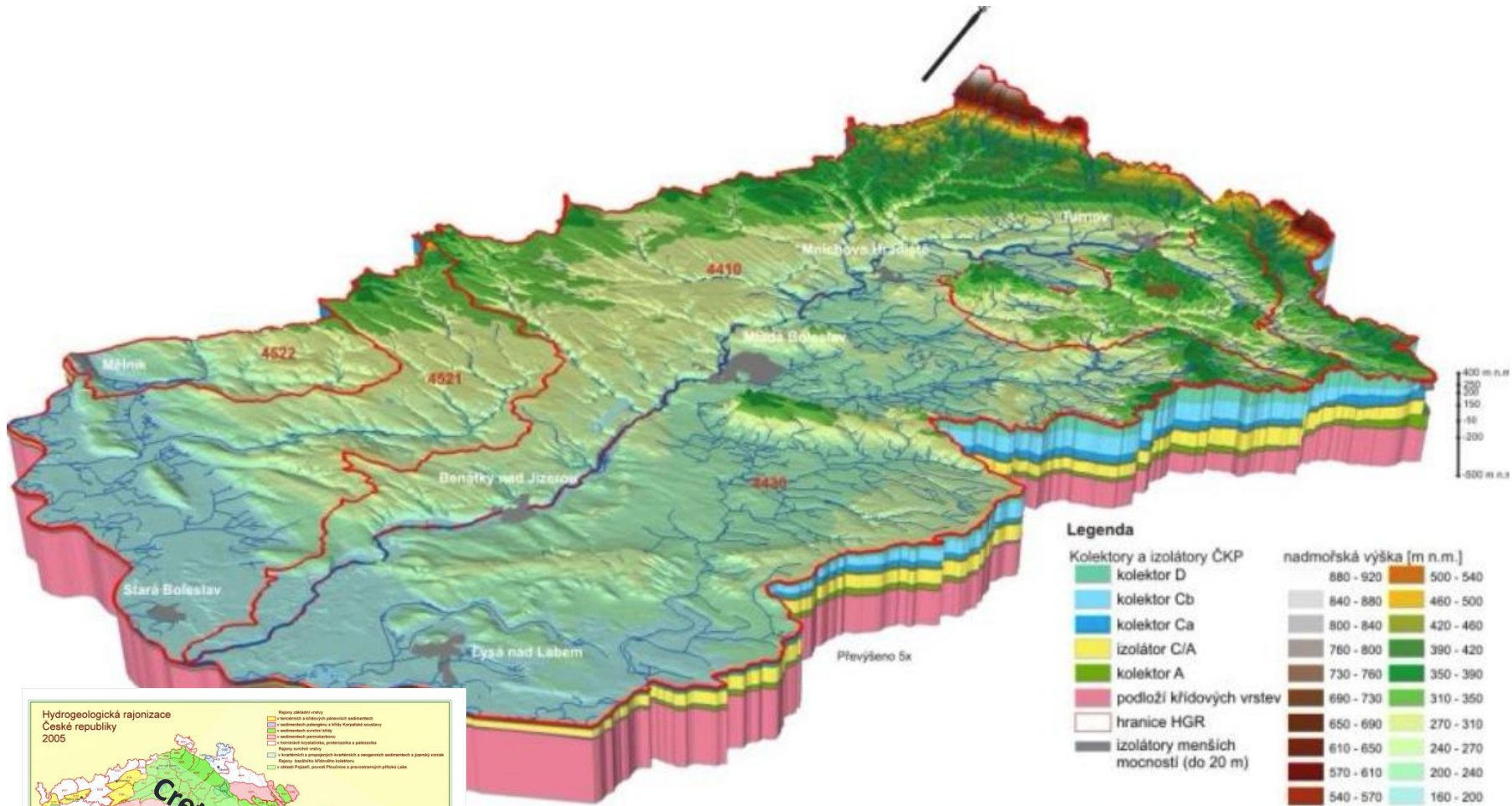
Potentiometric surface: Level to which over-pressured water will rise



Hydrogeological structures of CZ



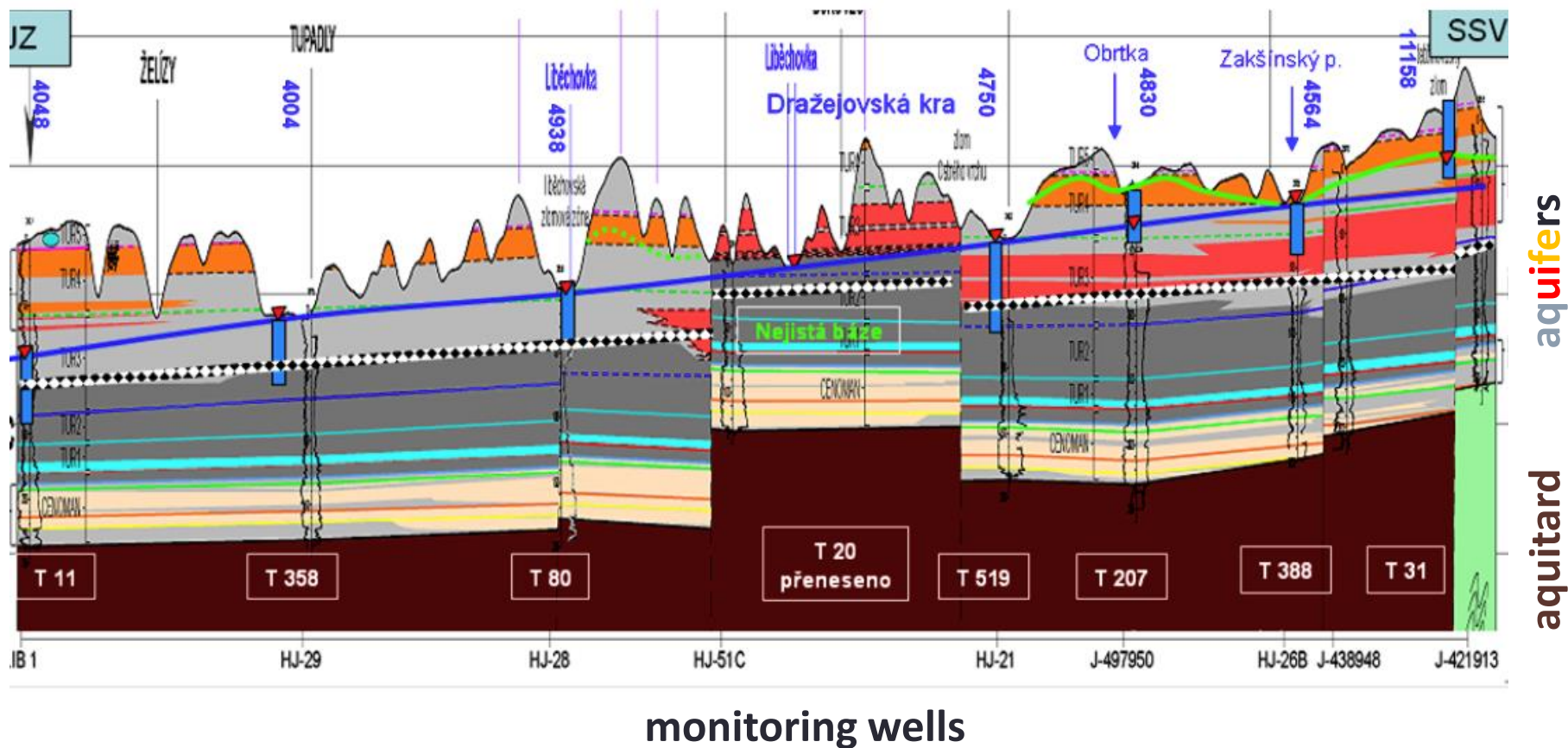
Detail of Jizera river aquifers in Cretaceous basin



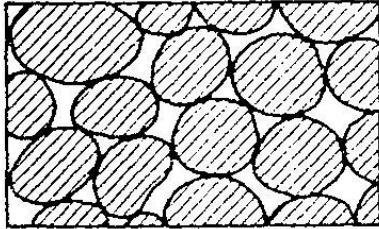
Kolektor in CZ=aquifer
Izolátor in CZ=aquitard

Cross-section of hydrogeological structure of upper Cretaceous basin in CZ, area of Kokořín

surface streams

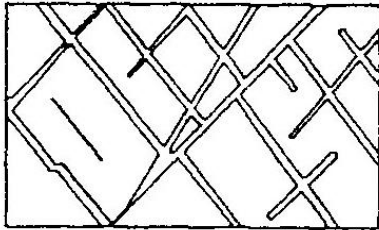


Types of permeability in aquifers (rock materials)

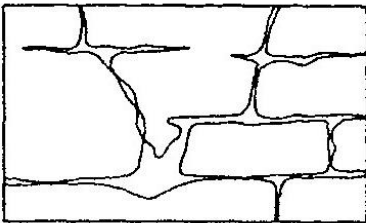


A

Matrix permeability
Clastic sediments free or
fortified (connected)



Fractures and fissures permeability
Igneous rocks



B

Karstic permeability
Soluble rocks – limestones, dolomites
or lava channels

Water balance

Sum of inflow – sum of outflow = change of volume in aquifer

Time frame for the inflows, outflow and change

Inflows to water bearing layer

Across horizontal boundaries

Between aquifers (or fractured bedrock)

Natural infiltration from precipitation

Returned water from irrigation

Artificial inflow

Lake and river discharge

Outflows to water bearing layer

Across horizontal boundaries

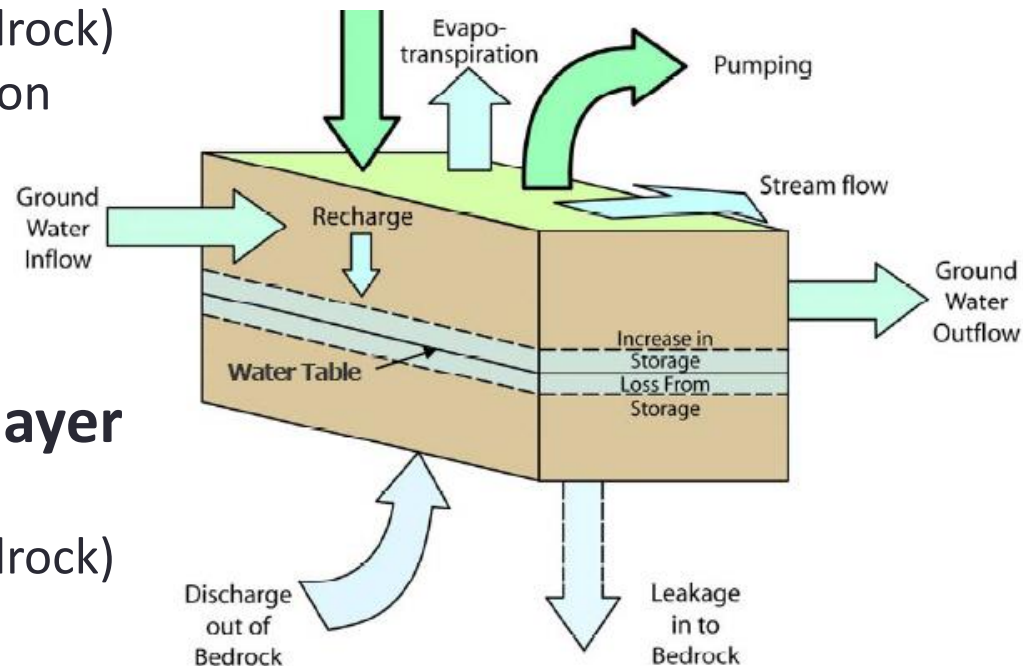
Between aquifers (or fractured bedrock)

Pumping, drainage

Seepage to rivers and lakes

Springs

Evapotranspiration



Magnitude of natural surplus of water to the aquifer relies on

Type of precipitation (water, snow, drizzle, storm, long light rain....)

Climate conditions (dry, wet, cold, hot)

Antecedent soil moisture

Topography

Vegetation cover

Infiltration as irrigation loss

20-40% of irrigation amount acc. To type of irrigation
(ponding worst, drip best)

Irrigation may activate latent pollution in the subsurface
or cause soil salinization

Artificial inflow

Process of addition of water into the aquifer in space and
time, managing water quantity and quality

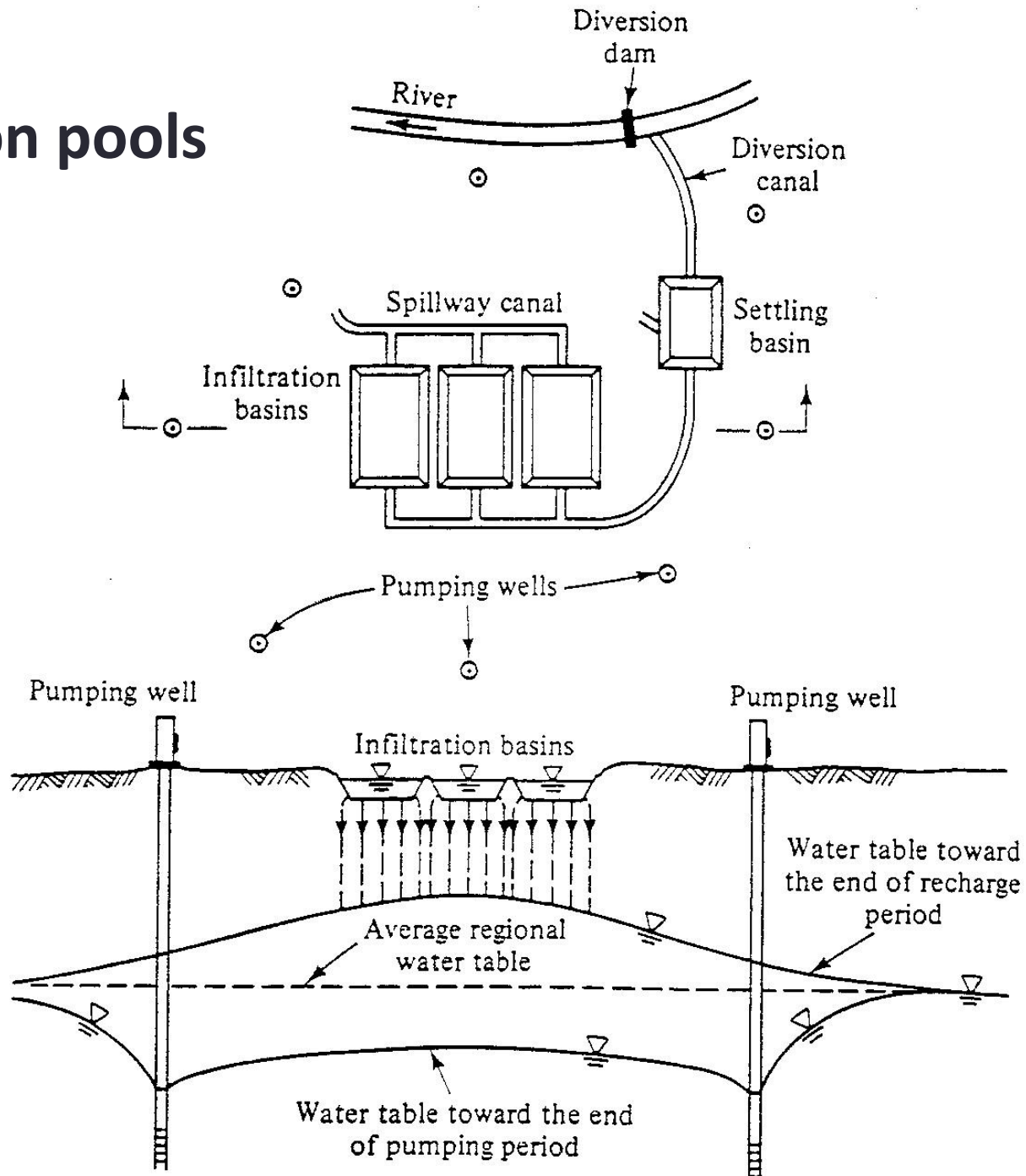
Aims:

- Hydrological regime management
- Water storage in porous media reservoirs
- Water quality management

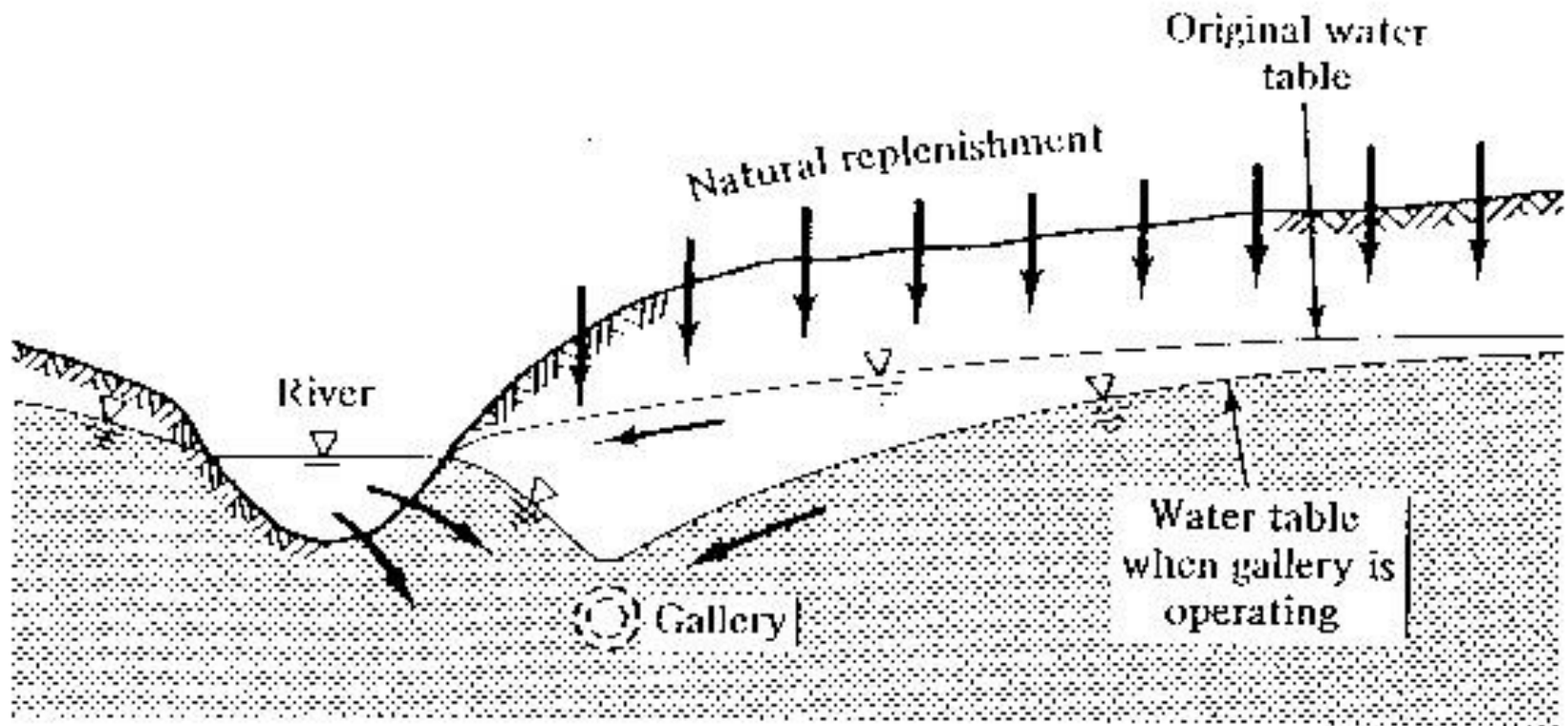
Methods:

- Increased infiltration in agriculture, small reservoirs
- Infiltration ponds and infiltration wells
- Induced inflow by horizontal pumping near surface
sources (water filtration)

Infiltration pools

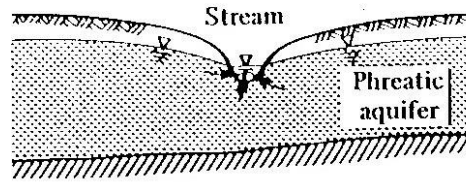


Increased inflow near collecting gallery

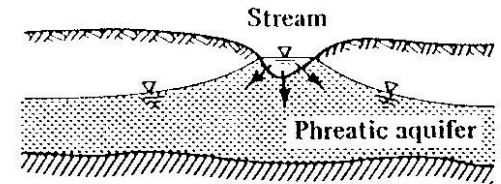


Interaction between surface water and aquifer

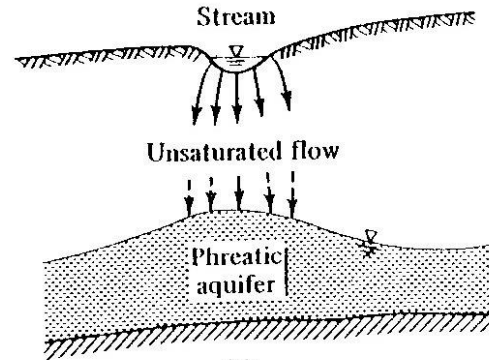
River can drain or feed
groundwater



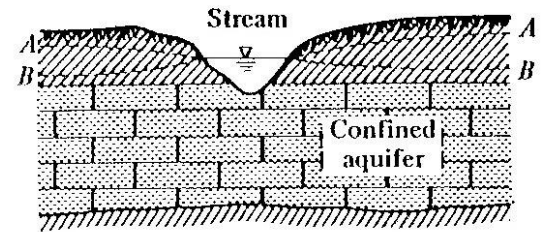
(a)



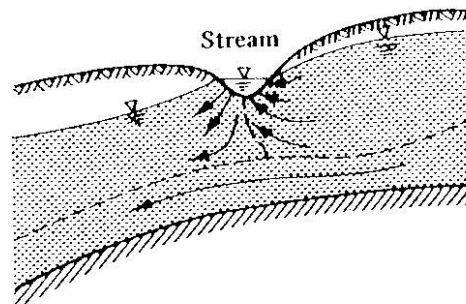
(b)



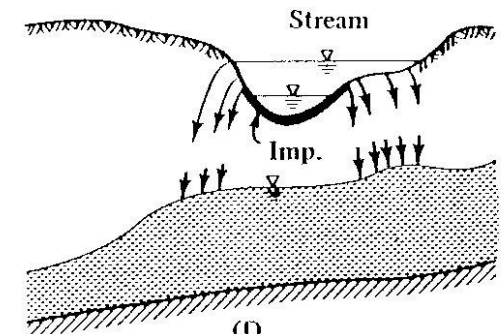
(c)



(d)



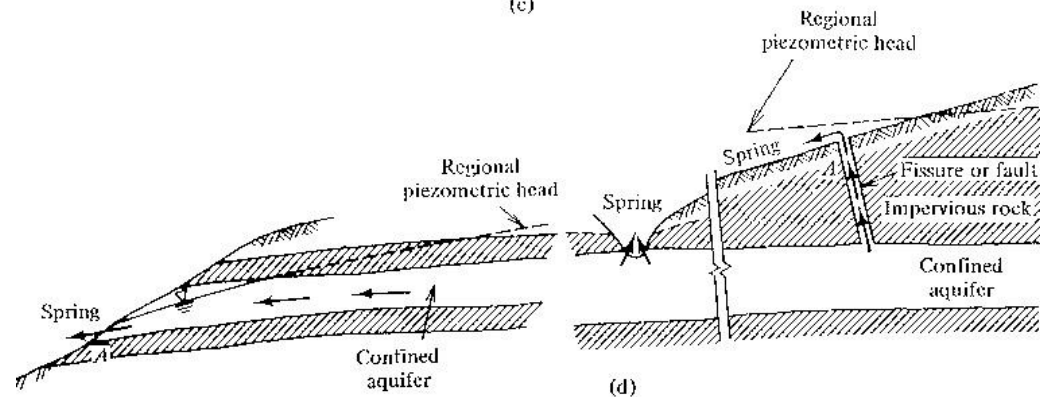
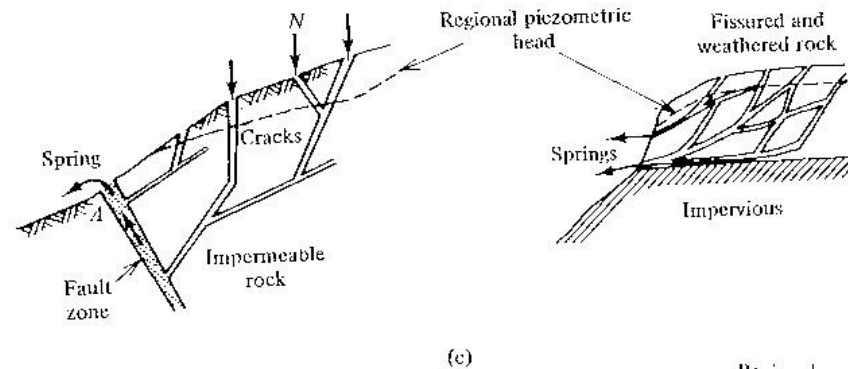
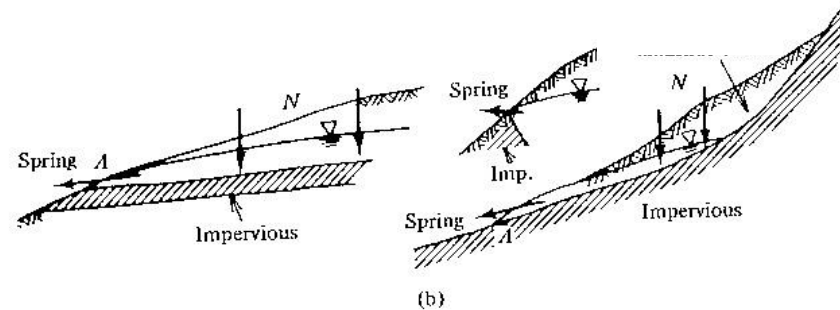
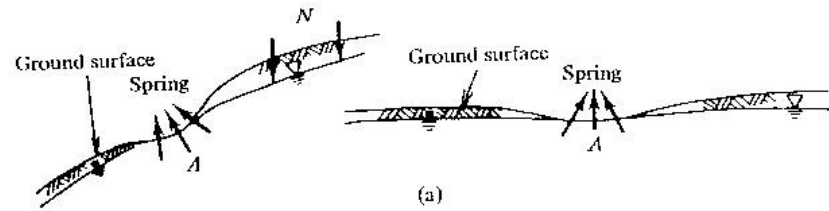
(e)



(f)

Springs

Springs with high water yield remarkably influence groundwater flow in surroundings



Evapotranspiration

Evaporation – loss of water from bare soil, open water or snow cover into the atmosphere

Transpiration - loss of water from soil by plants into the atmosphere

Evapotranspiration – total loss of water by combination of evaporation and transpiration

Potential evapotranspiration – possible when interface (soil surface) is fed by water fully all times

Actual evapotranspiration – based on meteorological factors (lower than potential)

Pumping and drainage

**Wells (point sink),
galleries, open ditches, subsurface drainage (line sink)**

Change of volume in aquifer

Free aquifer – increase of water table, confined aquifer – increase of pressure