



Seminar

HYDRUS 2D - introduction, setting up the domain, results visualization



Richards equation

$$\frac{\partial}{\partial x} \left(K_x(\theta) \frac{\partial h}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_y(\theta) \frac{\partial h}{\partial y} \right) + \frac{\partial}{\partial z} \left(K_z(\theta) \frac{\partial h}{\partial z} \right) + \frac{\partial K_z}{\partial z} = \frac{\partial \theta}{\partial t} \quad \dots \text{in } 3D$$

$$\frac{\partial}{\partial z} \left(K(h) \frac{\partial h}{\partial z} + K(h) \right) - S = \frac{\partial \theta}{\partial t}$$

van Genuchten

$$\theta_e(h) = \begin{cases} \frac{1}{\left(1 + (-\alpha h)^n\right)^m} & h < 0 \\ 1 & h \geq 0 \end{cases}$$

Mualem

$$K_r(\theta_e) = \theta_e^{1/2} [1 - (1 - \theta_e^{1/m})^m]^2$$

Theory repetition



$$\frac{\partial \theta}{\partial t} = - \frac{\partial q}{\partial z} - s = \frac{\partial}{\partial z} \left[K \left(\frac{\partial h}{\partial z} + 1 \right) \right] - s$$

Advection dispersion eq. as implemented in HYDRUS

$$\frac{\partial \theta c}{\partial t} + \frac{\partial \rho s}{\partial t} = \frac{\partial}{\partial z} \left(\theta D \frac{\partial c}{\partial z} \right) - \frac{\partial qc}{\partial z} - \overset{\text{Sink (flow)}}{Sc_r} - \overset{\text{Reactions (decay)}}{\mu_w \theta c - \mu_s \rho s + \gamma_w \theta + \gamma_s \rho}$$

c – solute concentration in liquid phase

s – solute concentration on solid phase

Molecular diffusion coef.

Long. dispersivity (*input*)

Dispersion coefficient

$$D = D_w \tau + \lambda |v|$$

Tortuosity factor

Mean pore velocity

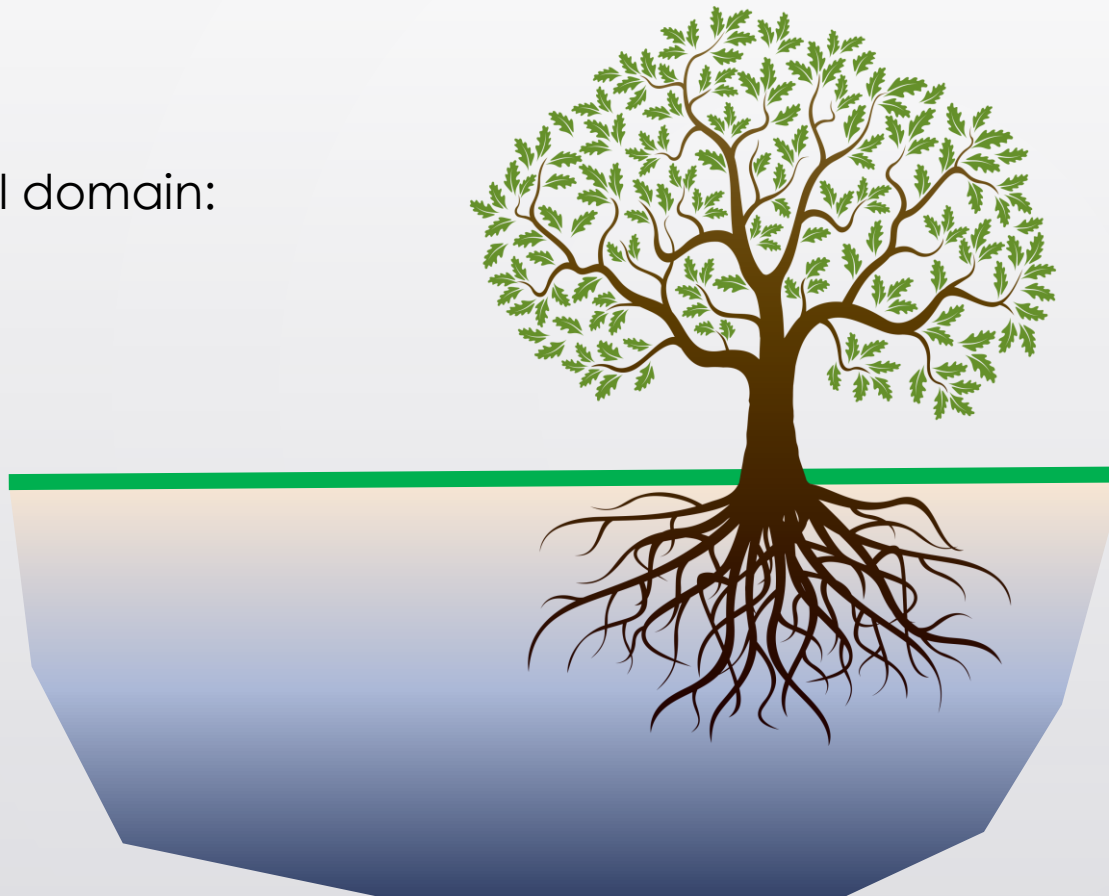
Equilibrium adsorption:

$$s = k_d c^\beta / (1 + \eta c^\beta)$$

Distribution coeff.

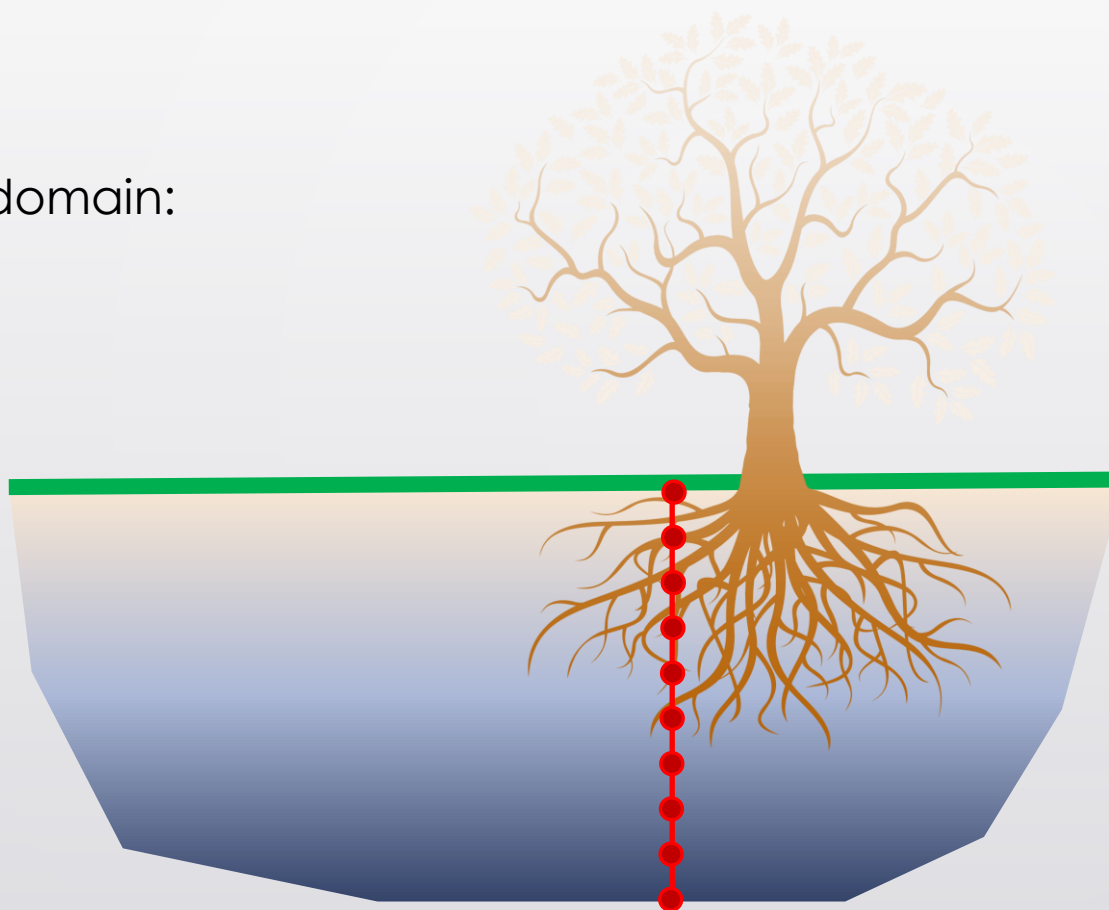
Discretization in 1D

Real domain:



Discretization in 1D

1D domain:



Top boundary node

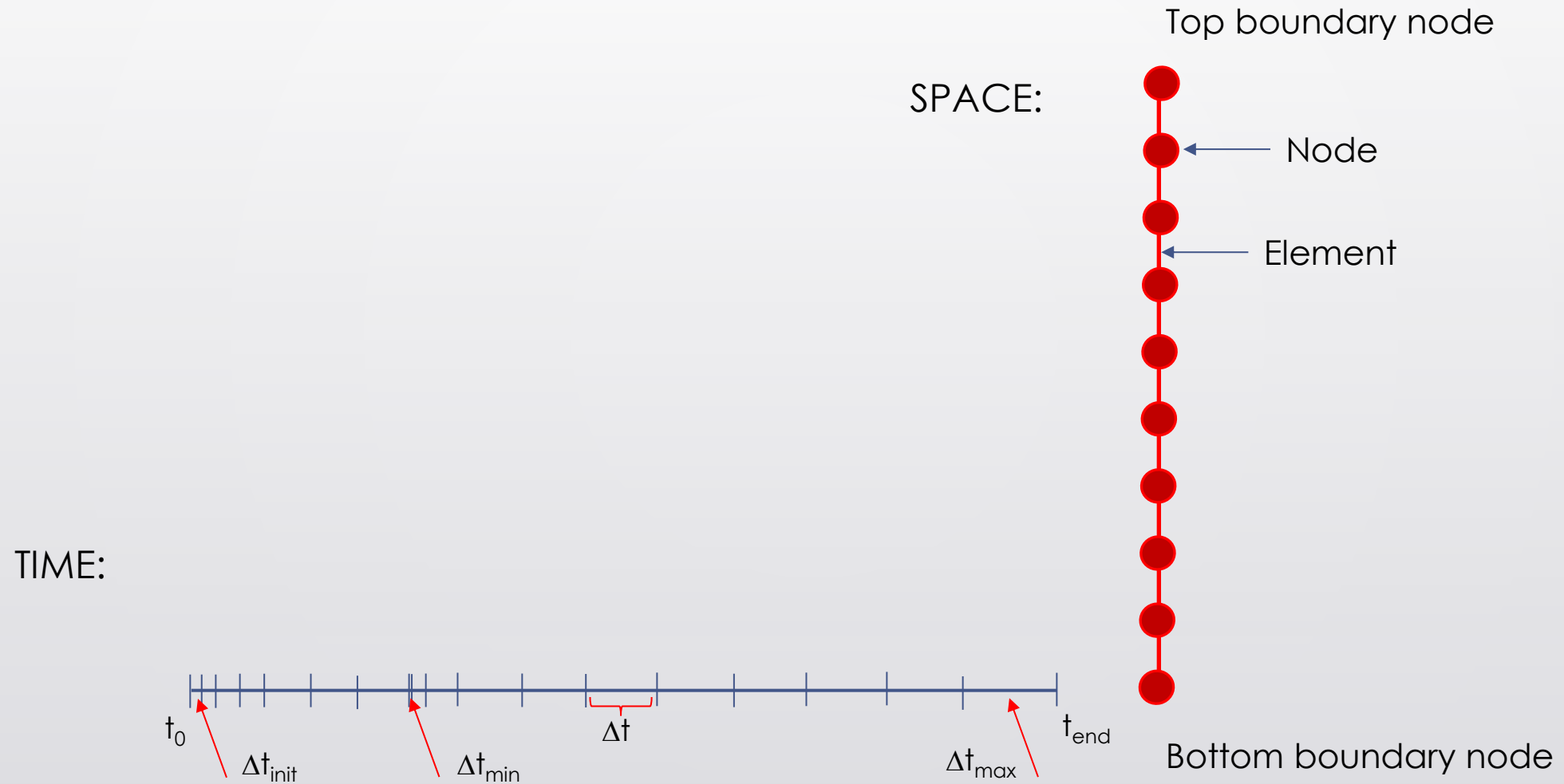


Node

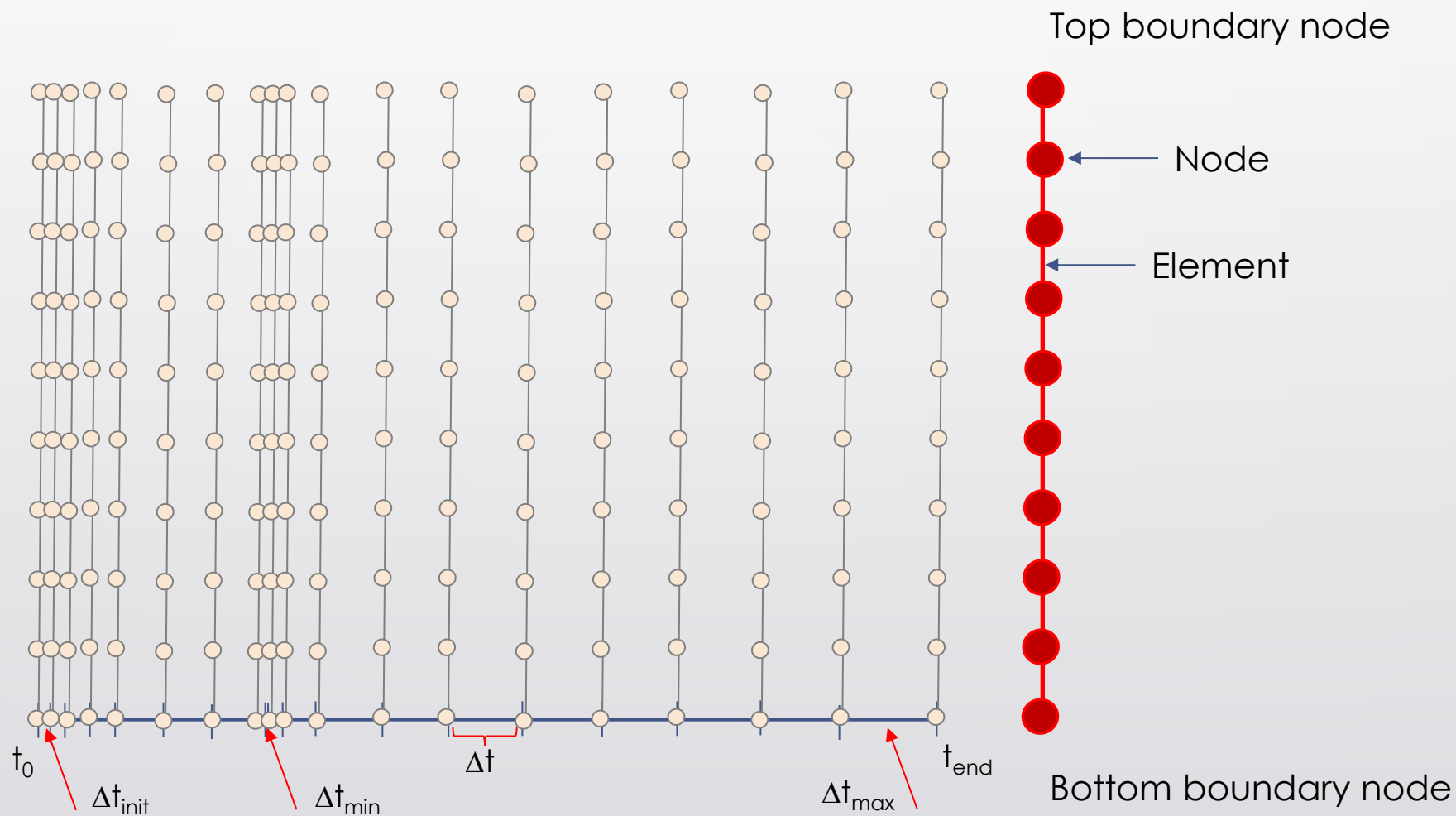
Element

Bottom boundary node

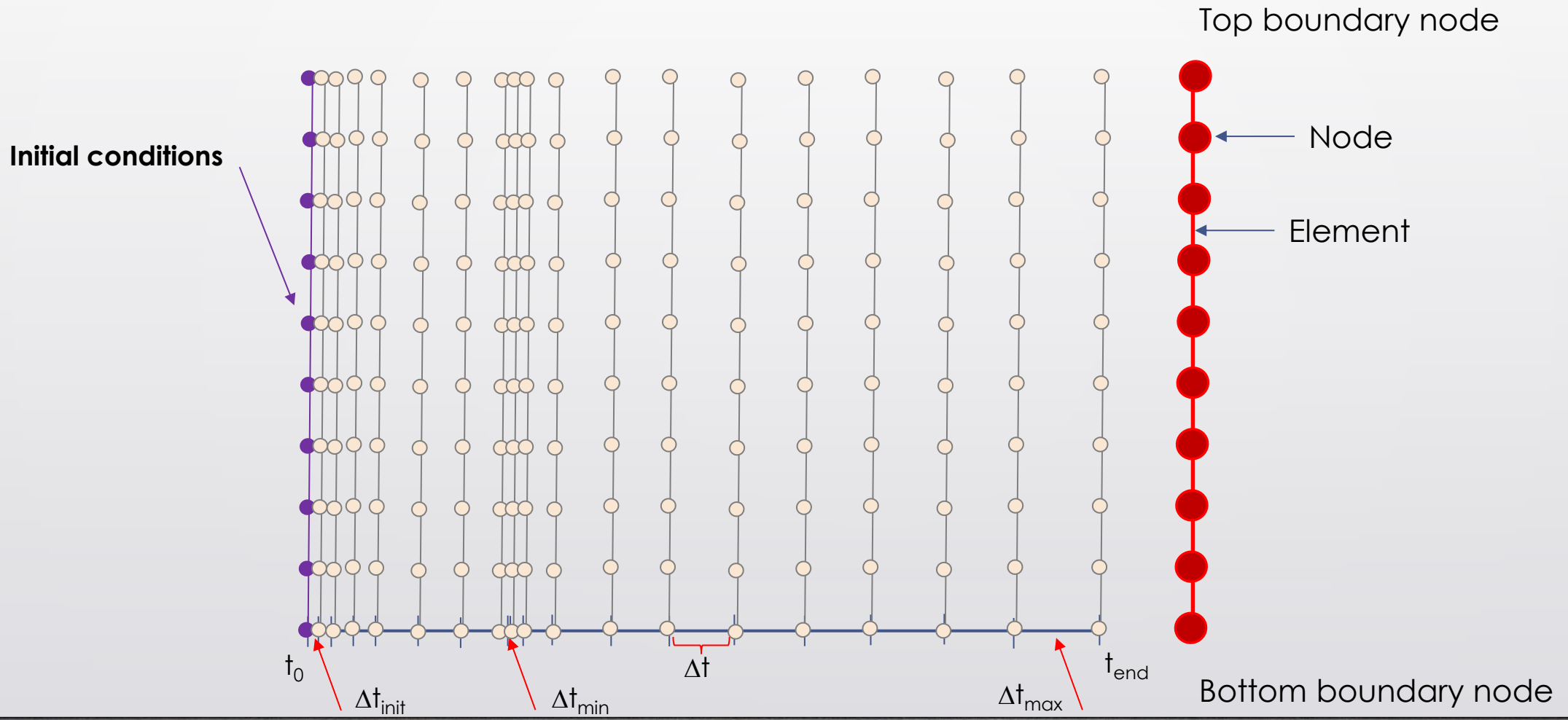
Discretization in 1D



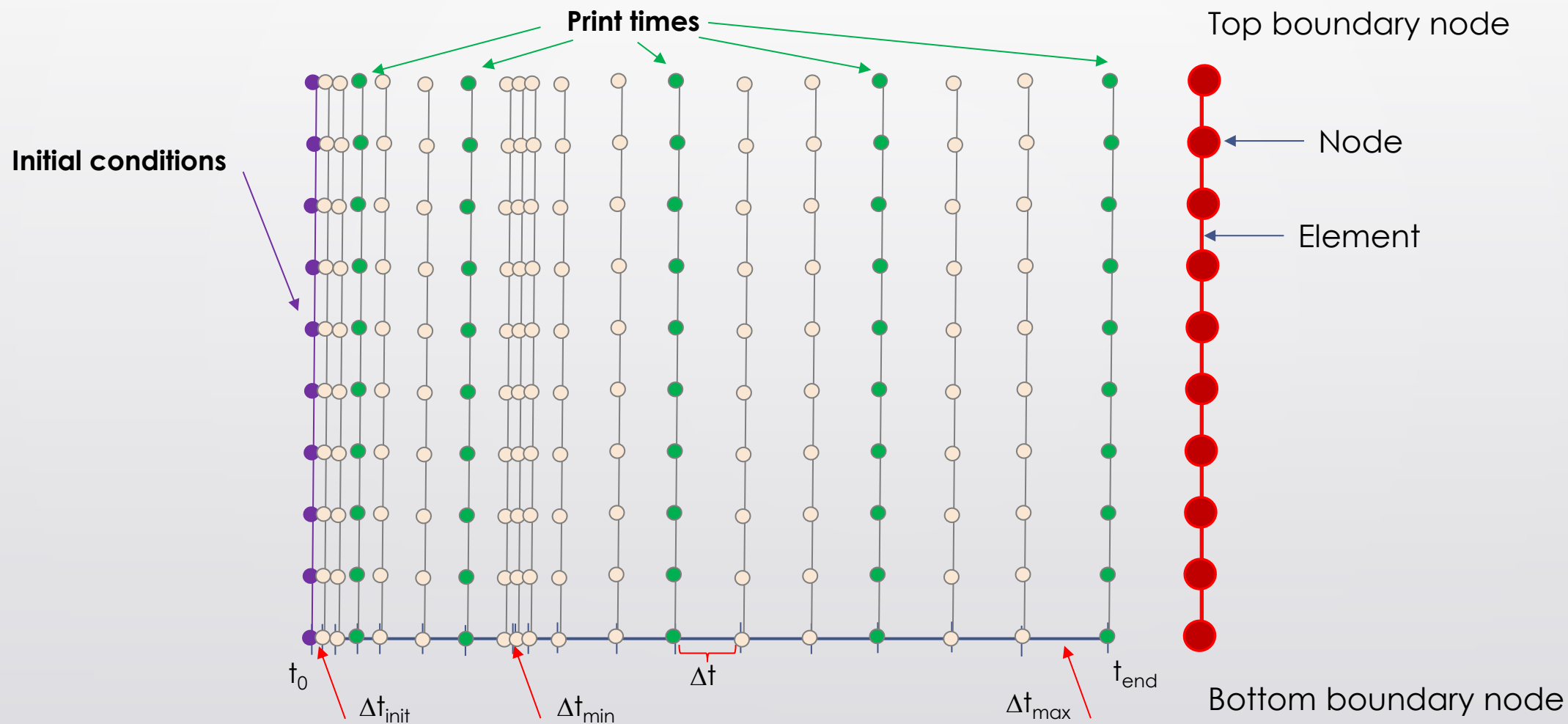
Discretization in 1D - calculation matrix



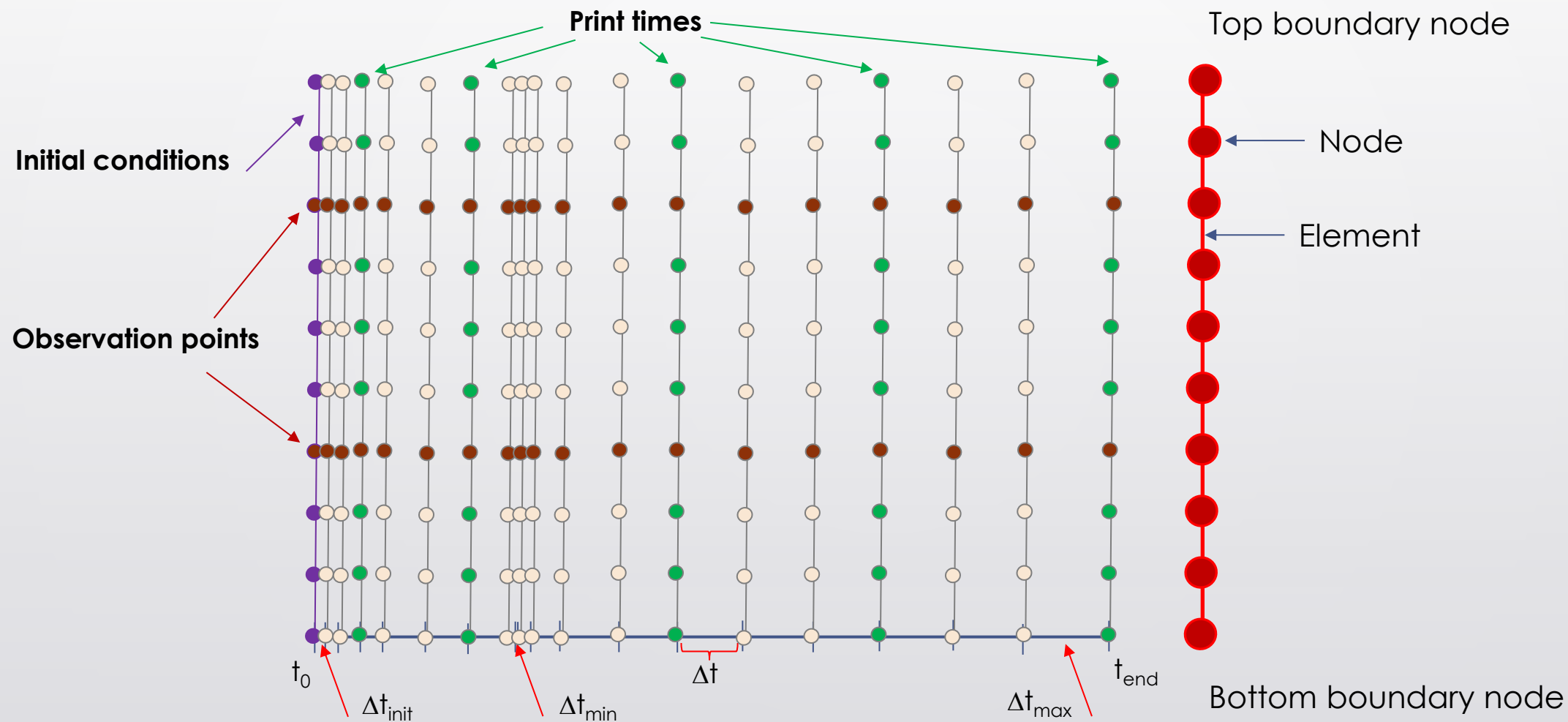
Discretization in 1D - calculation matrix



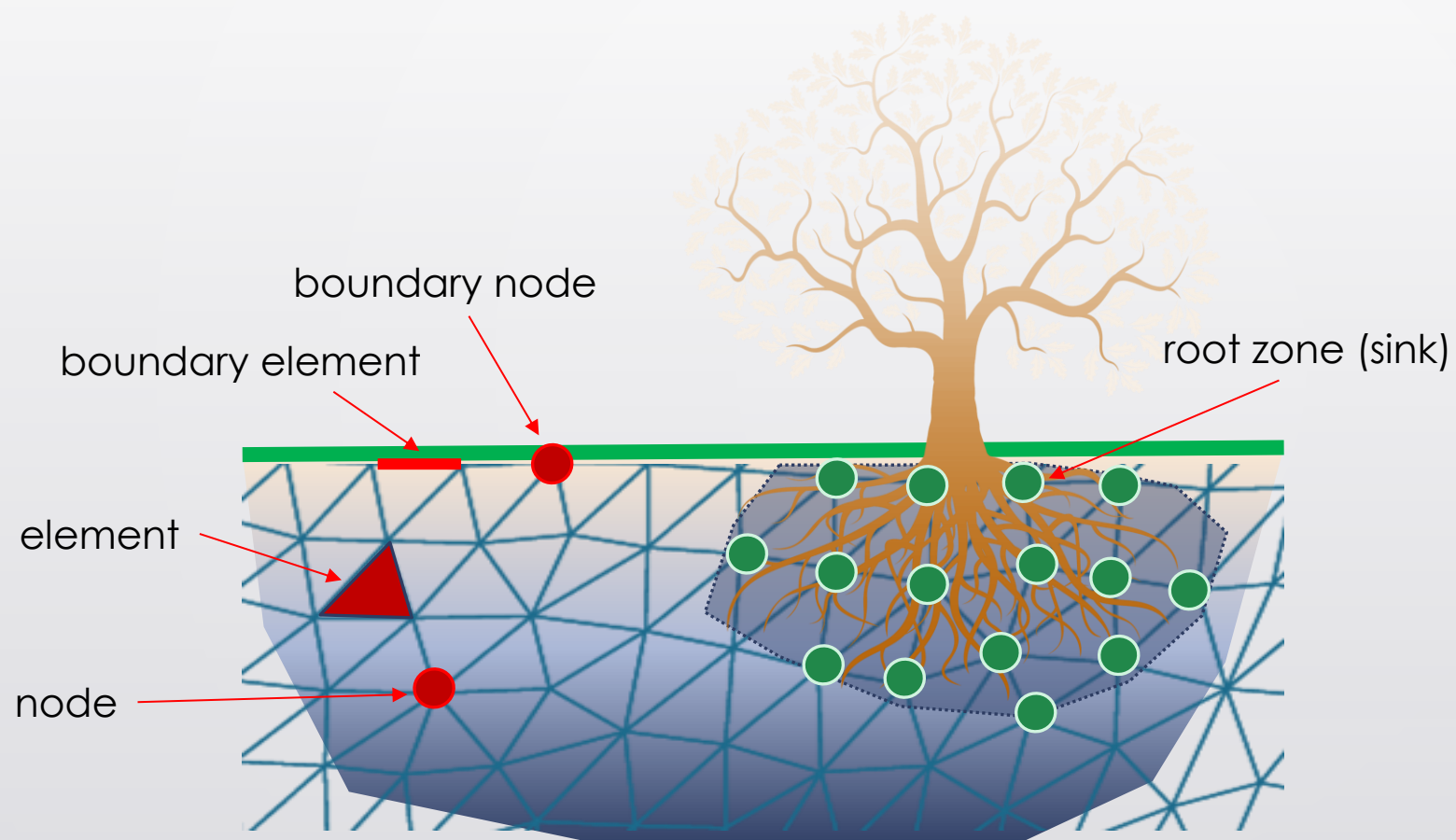
Discretization in 1D - calculation matrix



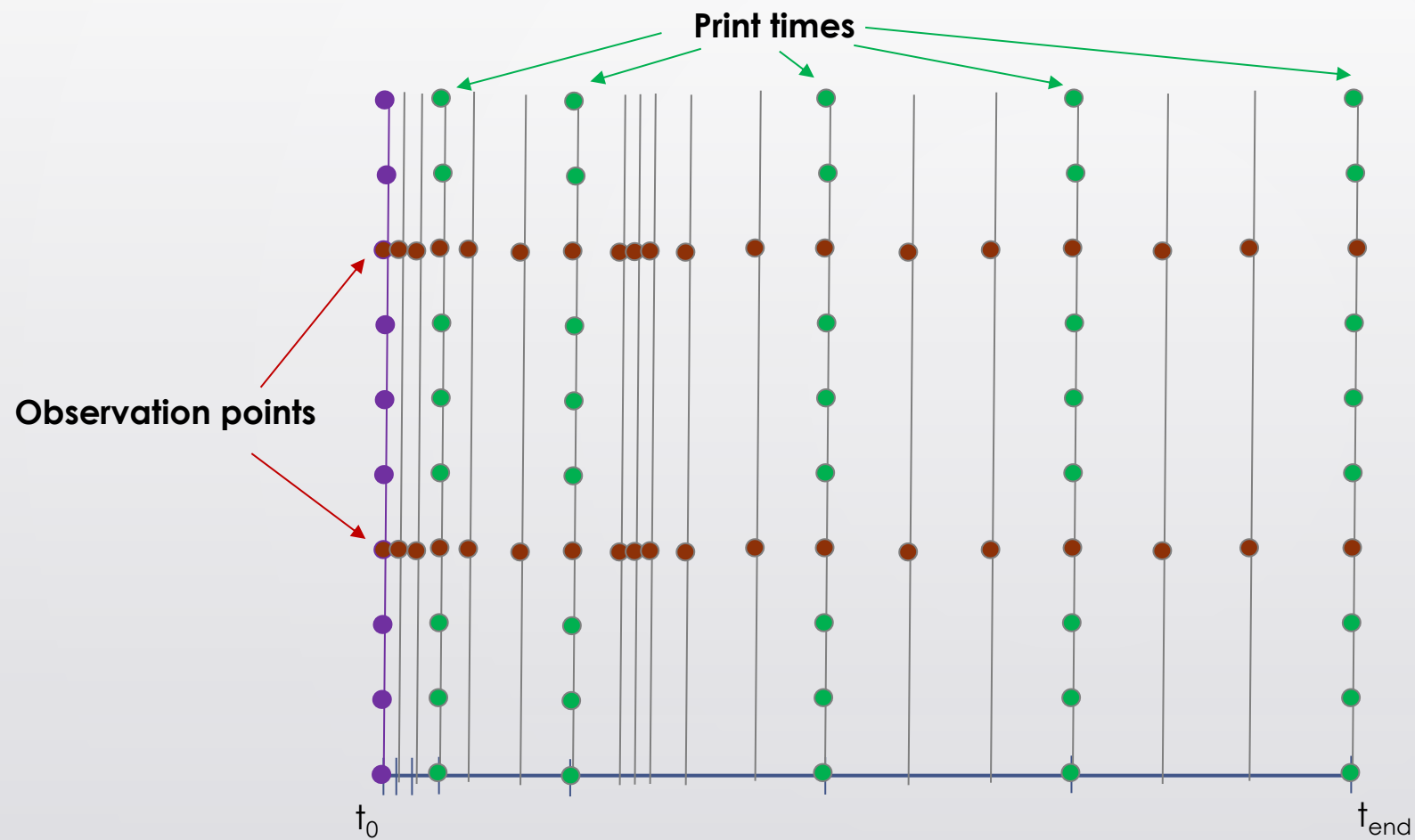
Discretization in 1D - calculation matrix



Discretization in 2D



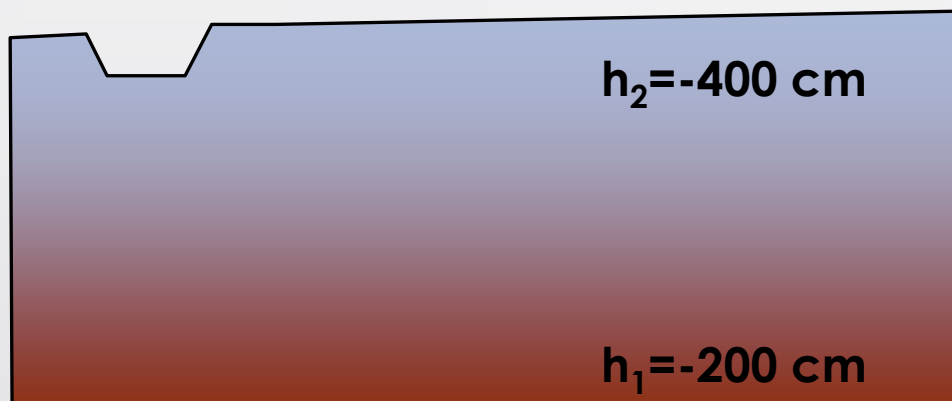
Discretization in 1D - results



Initial conditions

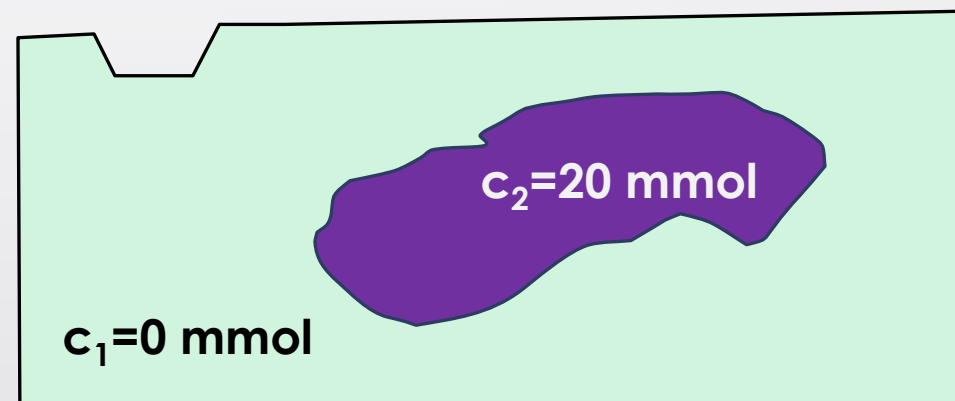
Richards eq.:

Matric potential / water content distribution

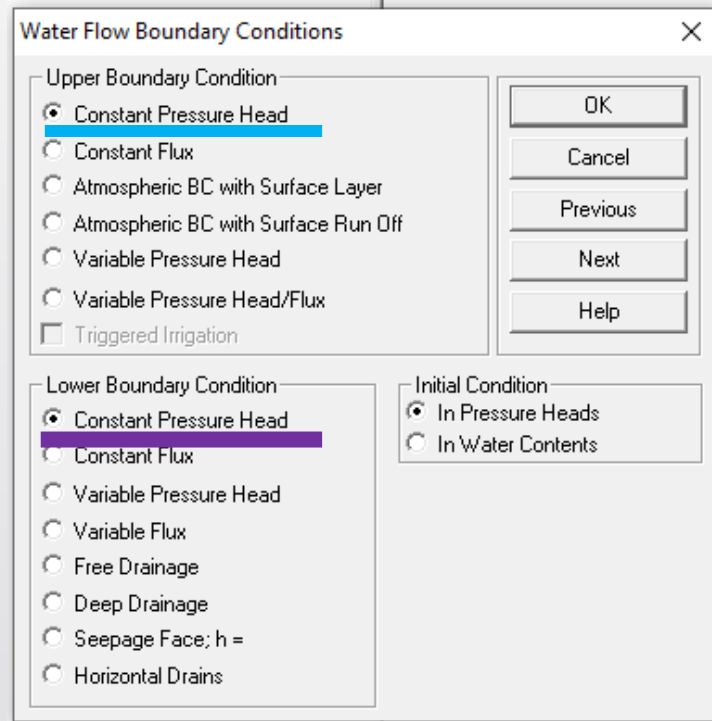


ADE:

Initial solute concentration distribution

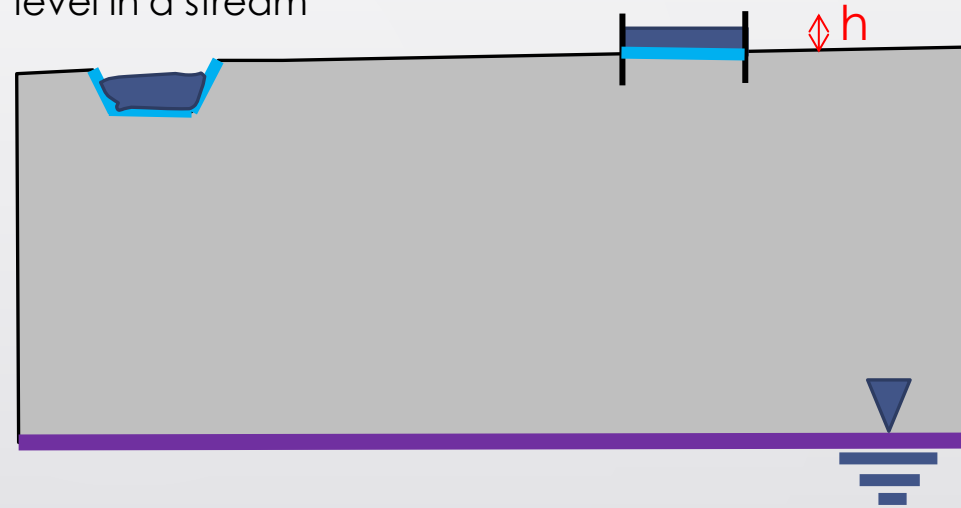


Boundary conditions - Repetition



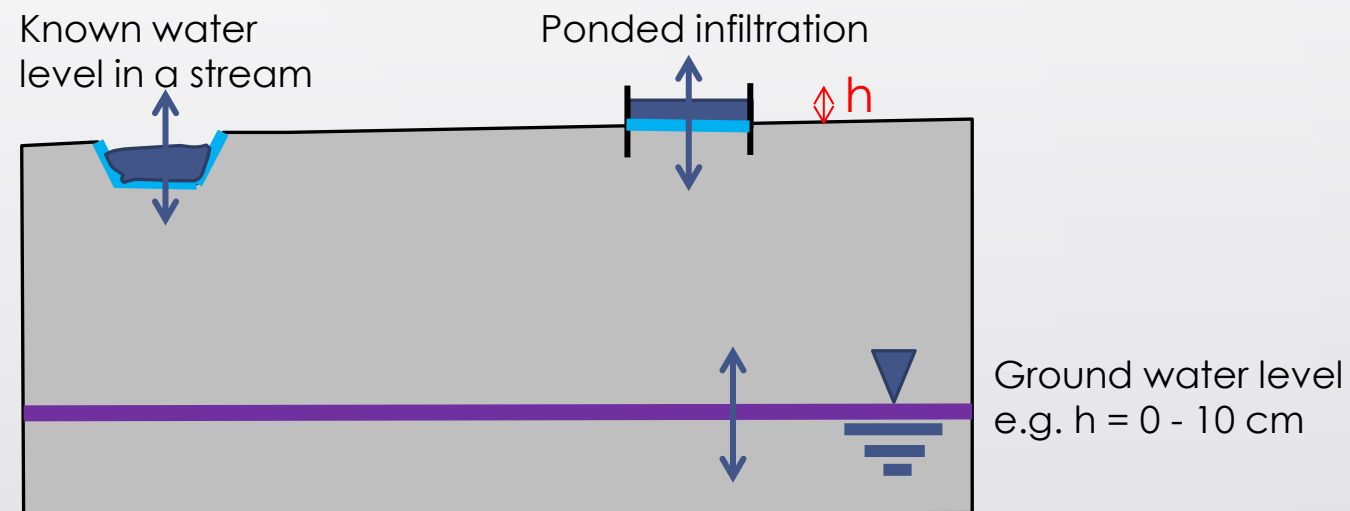
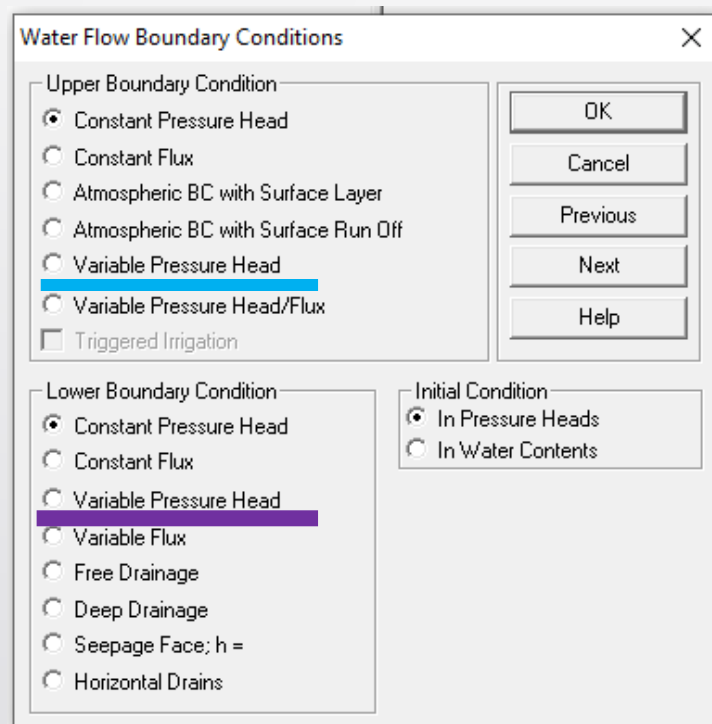
Known water
level in a stream

Ponded infiltration

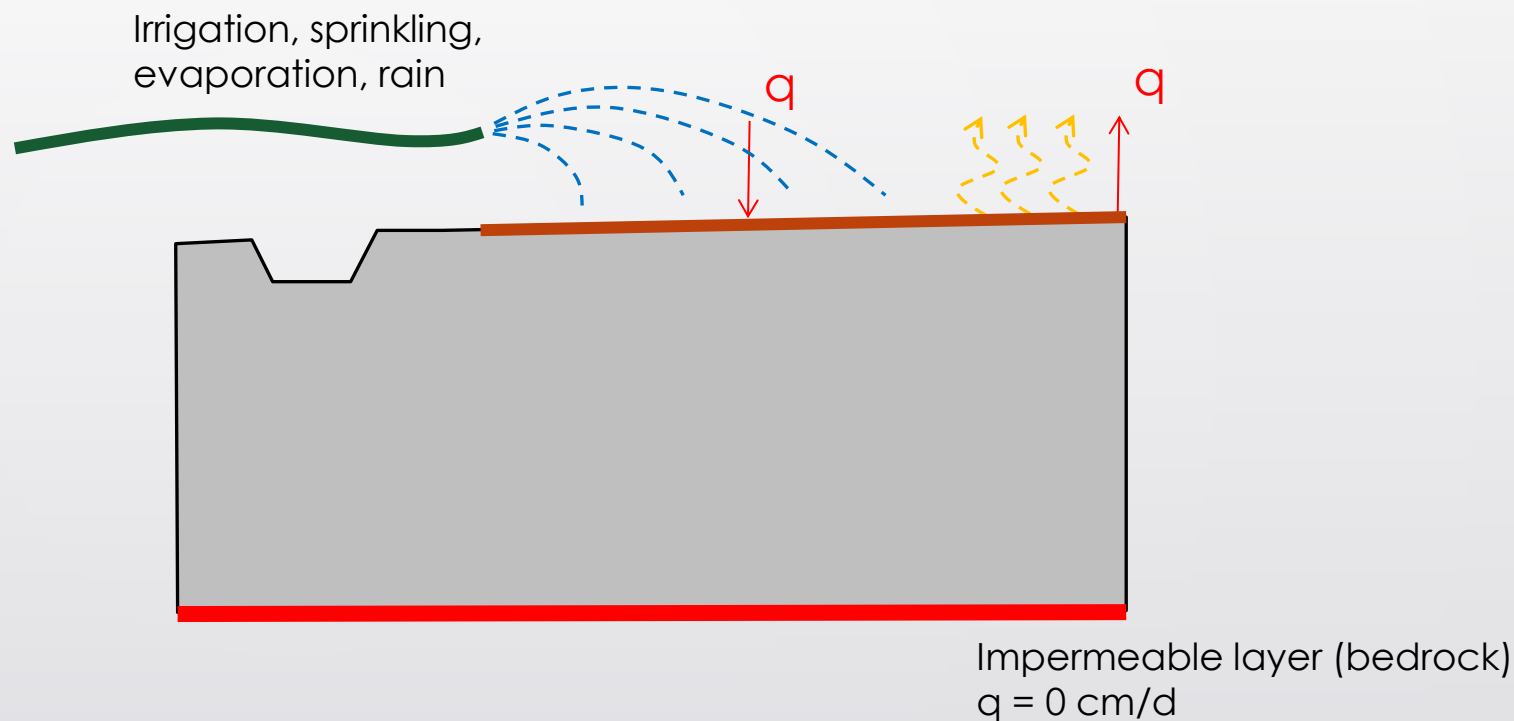
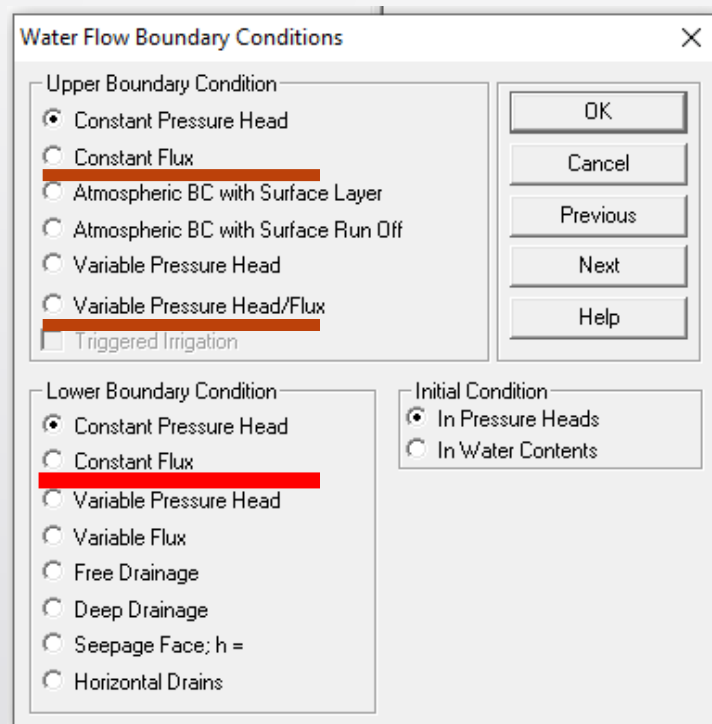


Ground water level
e.g. $h = 0$ cm

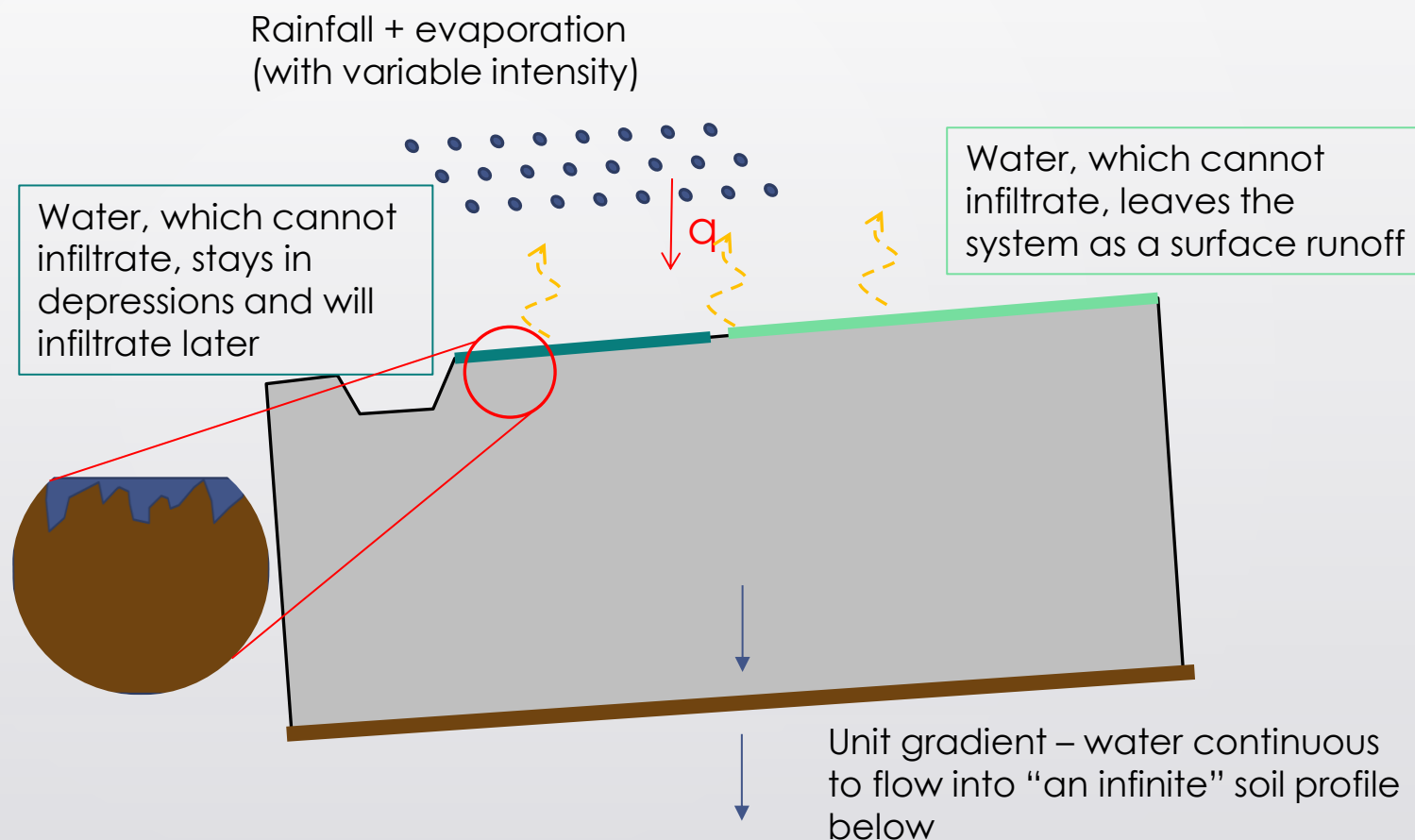
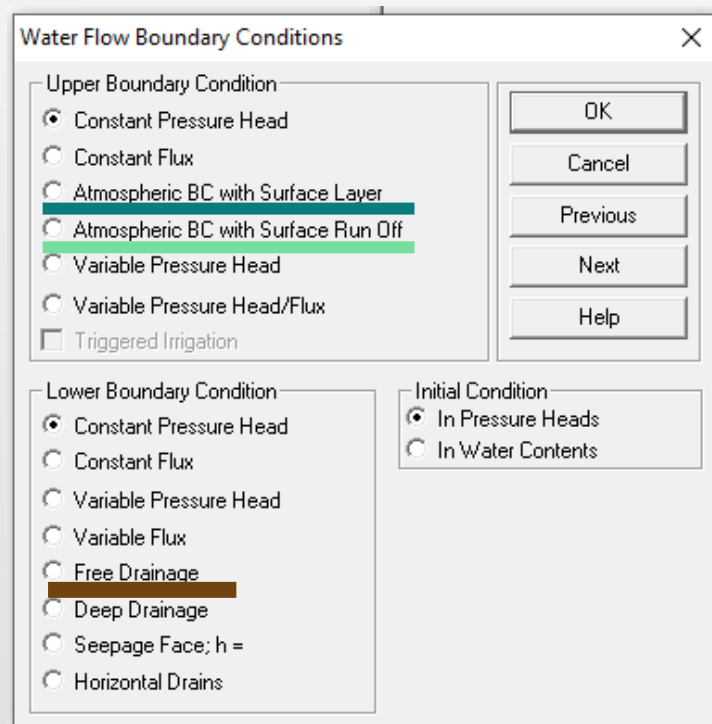
Boundary conditions



Boundary conditions



Boundary conditions



Boundary conditions

Water Flow Boundary Conditions

Upper Boundary Condition

- ☒ Constant Pressure Head
- ☐ Constant Flux
- ☐ Atmospheric BC with Surface Layer
- ☐ Atmospheric BC with Surface Run Off
- ☐ Variable Pressure Head
- ☐ Variable Pressure Head/Flux
- ☐ Triggered Irrigation

Lower Boundary Condition

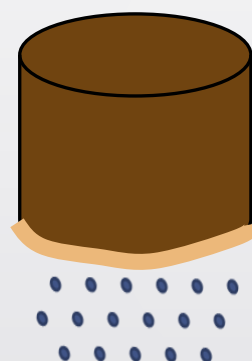
- ☒ Constant Pressure Head
- ☐ Constant Flux
- ☐ Variable Pressure Head
- ☐ Variable Flux
- ☐ Free Drainage
- ☐ Deep Drainage
- ☐ Seepage Face; $h =$
- ☐ Horizontal Drains

Initial Condition

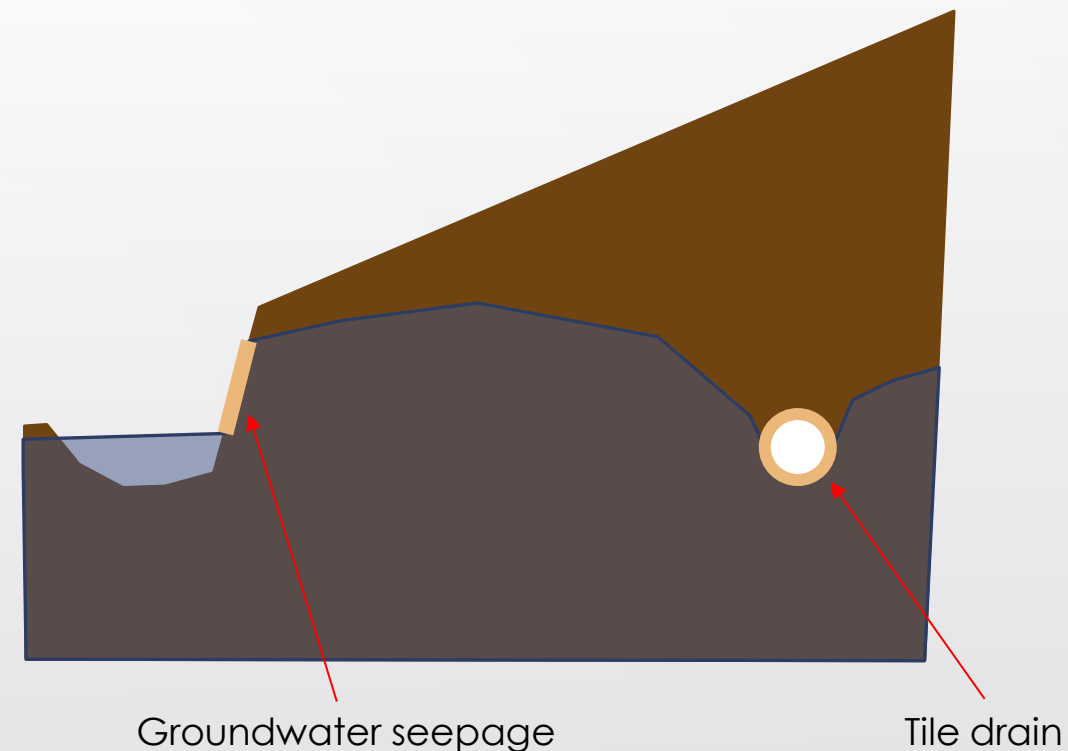
- ☒ In Pressure Heads
- ☐ In Water Contents

OK Cancel Previous Next Help

Interface between soil and atmosphere



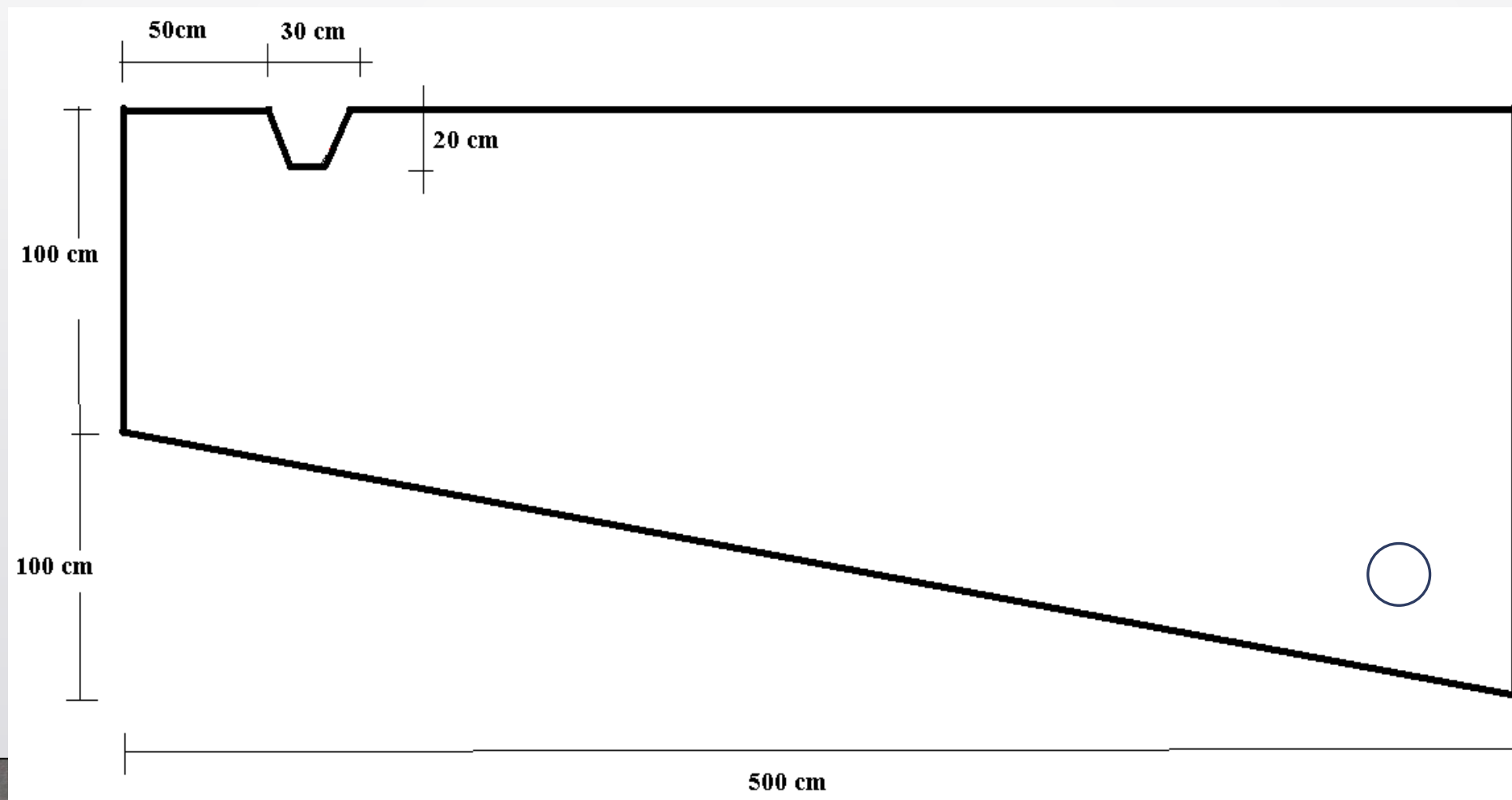
Lab soil sample



Groundwater seepage

Tile drain

Ditch infiltration with impermeable bottom boundary



Ditch infiltration with impermeable bottom boundary

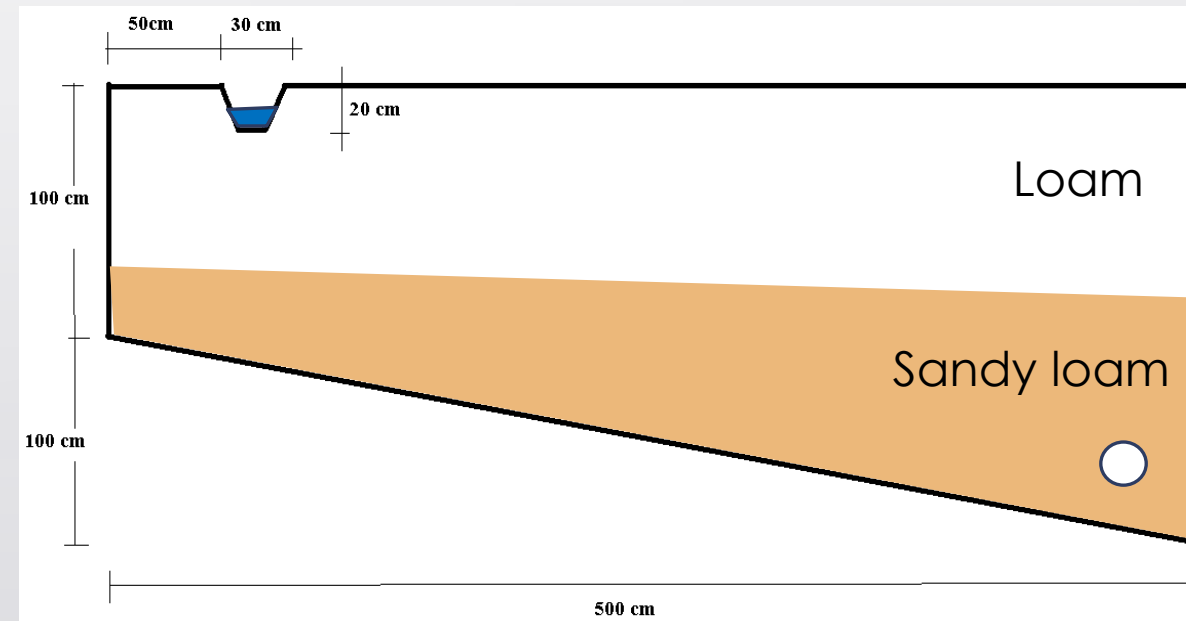
The ditch was filled with 8 cm of water.

Initial conditions: pressure 0 cm at the lowest point of the domain, the rest in equilibrium

Boundary conditions: no flux – everywhere except the ditch and the tile drain

Duration: 50 days

Soils: upper horizon *loam*, bottom layer *sandy loam*
(use catalogue soil hydraulic properties)



Ditch infiltration with impermeable bottom boundary

Transport:

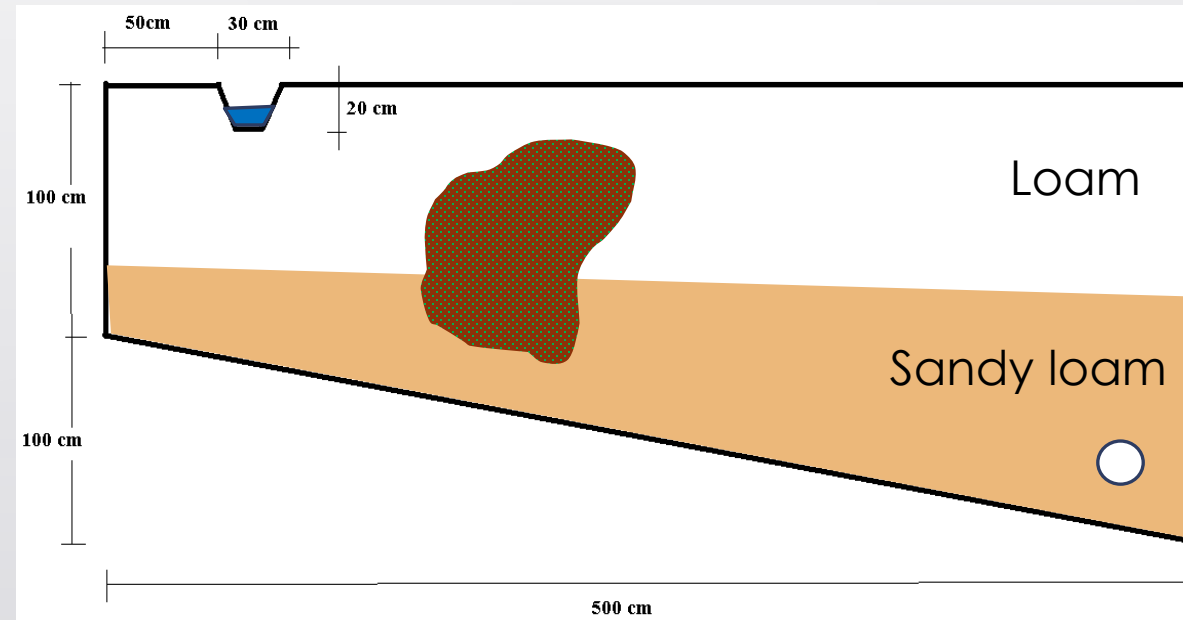
1. Simulate a conservative tracer, dissolved in infiltrating water for a duration of 1 day, conc. 5 mg/cm².
2. Consider solute B already located in the simulated domain (pick a location between the ditch and drainage). $k_d = 1.1$, conc. 10 mg/cm².

Dispersivity in both directions: 40 cm

Topsoil bulk density: 1.28 g/cm³, bottom 1.40 g/cm³

Print information: select 200 print times with time step of 6 hours

Flowing particles: Insert 5 – 15 flowing particles (few close to the ditch, rest as you wish)



Ditch infiltration with impermeable bottom boundary

- a/ Observe, how is the domain being filled with water and how do the solutes propagate.
- b/ Identify locations with the highest velocities.
- c/ How much water/solutes were infiltrated and recovered via the drainage after 10 and 50 days?
- d/ How much solutes remain in the domain after 50 days?

